<u>IMPORTANT QUESTION & ANSWERS</u> UNIT –I FLUID PROPERTIES AND FLOW CHARACTERISTICS PART-B

- 1. A 15 cm diameter Vertical cylinder rotates conventically Inside another cylinder of diameter 15, 10 cm. Both cylinders are 25 cm high. The Space between the cylinders is filled with a liquid whose Viscosity is Unknown. If a tarque of 12.0 Nm is sequired to rotate the Inner cylinder at 100 H.p.m. determine the Viscosity of the fluid. IS Given: Calculate the Power? I May / June - 2013] Diameter of evender - 15 cm = 0.15 m
 - Diameter of cylinder = 15cm = 0.15m Dia. of outer cylinder = 15.10cm = 0.151m length of cylinders, L = 25cm = 0.25m. Torque T = 12 Nm. Speed N = 600 M.p.m.

To Find ;

Vixconity M=?; Power (P)=?

Formula ;

 $M = \frac{T}{\frac{du}{\frac{dy}{d$

Solution !

(i) Tangential Velouity of Cylinder $U = \frac{TDN}{b0}$ $U = \frac{TXD.15 \times 100}{60} \Rightarrow 0.7854 \text{ m/s.}$ (ii) Scotlace area of Cylinder, A = TDXL

$$A = \overline{11} \times 0.15 \times 0.25 = 0.1178.$$

$$dy = \frac{0.151 - 0.15}{2} = 0.0005 \text{ m}.$$
Shear Atness (T) = $M. \frac{du}{dy}$

$$\overline{T} = \frac{M \times 0.7854}{0.0005}$$
Shear yonce = Shear Gliens × Area.(A)
CF)
$$Torque (T) = F \times D/2$$

$$I2 = F \times (\frac{0.15}{2})$$

$$F = \frac{12}{0.075} \Rightarrow 160 \text{ N}.$$

$$\overline{F} = 160 \text{ N}.$$
Shear (T) = $\frac{F}{A}$

$$= \frac{160}{0.1178} \Rightarrow 1358.28.$$

$$\overline{T} = 1358.23 \text{ N/m}^2$$

. .

•

Visconity
$$(M) = \frac{\overline{c}}{\left(\frac{du}{dy}\right)}$$

 $\overline{c} = 1358 \cdot 23 \ N/m^2$
 $M = \frac{1358 \cdot 23}{\left(\frac{0.7854}{0.0005}\right)} \Rightarrow 0.864 \ Ns/m^2$. -
Visconity $M = 0.864 \ Ns/m^2$ (or)
 $= 0.864 \ \times 10 \Rightarrow 8.64 \ Poise$.
Power (P) = $2\overline{ti} N \overline{t}$
 $= \frac{2 \times \overline{ti} \times 100 \times 12}{60}$

The Velocity distribution over a plate is given by the selation, $u = y\left(\frac{2}{3} - y\right)$; where y is the Vertical distance above the plate in meters. Assuming a distance above the plate in meters. Assuming a Viscosity of 0.9 Pa.s. find the shear stress at 2. Y=0 and y=0.15m. [NOV - Dec - 2012]

3

Given:
Velouity
$$(u) = y (2/3 - y) (0x) e = \frac{1}{10} \frac{NS}{m^2}$$

distribution
 $\frac{2}{3}y - y^2$.
 $e = \frac{0.9}{(0)}$
 $= 0.09 Nc/m^2$]

To Find :

Shear Stress at a distance y = 0; y=0,15m

Formula required:

Solution;

$$u = \frac{g}{g} y - y^2 \cdot [dy]_{..} w.r.t y]$$

we get,

$$\frac{du}{dy} = \frac{2}{3} - 2y.$$

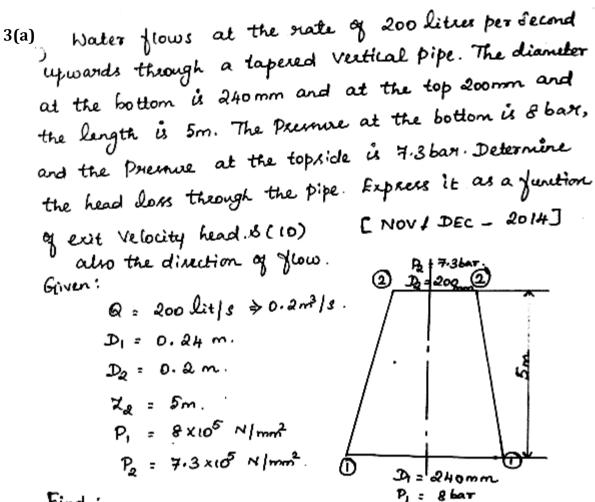
 $\begin{array}{rcl} \mathcal{A}t & y = 0 & ; \\ \frac{du}{dy} &= \frac{2}{3} - 2(0) \\ \frac{du}{dy} &= \frac{2}{3}/s \end{array}$

(i) Shear stress
$$(T)_{y=0} = 0.06 \text{ N/m}^2$$

(i) Shear stress $(T)_{y=0} = n.(\frac{du}{dy})(\frac{du}{dy})$
 $= 0.09 \times \frac{2}{3}$
At $y = 0.15$,
 $\frac{du}{dy} = \frac{2}{3} - 2(0.15)$
 $= 0.36/s$.
 $(T)_{y=0.15} = 0.09 \times 0.36$
 $= 0.033 N/m^2$.

Result :

(i) Sheart Stress at
$$y=0 = 0.06 \text{ N/m}^2$$
.
(ii) Sheart Stress at $y=0.15 \text{ m}$
(ii) Sheart Stress at $y=0.15 \text{ m}$
(i) $y=0.033 \text{ N/m}^2$



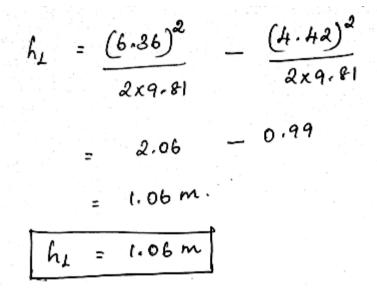
Find :

(i) Head Loss (hr) = ? (ii) Direction of Yloco : ? Formula required :

$$\frac{p_{i}}{Pg} + \frac{v_{i}^{2}}{2g} + z_{i} = \frac{p_{2}}{Pg} + \frac{v_{a}^{2}}{2g} + z_{2} + h_{L}.$$

dolution:

$$\frac{\frac{P_{1}}{P_{g}} + \frac{V_{1}^{2}}{2g} + z_{1}}{\frac{P_{g}}{P_{g}} + \frac{V_{g}^{2}}{2g}} + \frac{V_{g}^{2}}{2g} + z_{2} + h_{L}}{\frac{8 \times 10^{5}}{P_{g}} + \frac{V_{1}^{2}}{2g}} + 0 = \frac{\frac{7.3 \times 10^{5}}{P \times g} + \frac{V_{2}^{2}}{2g}}{\frac{P_{\chi}}{P_{\chi}}} + \frac{V_{2}^{2}}{2g}} + \frac{5 + h_{L}}{2g} + \frac{5}{2}$$



(i) Direction of
$$flow$$
.
 $E_A = E_B + h_L \qquad \begin{bmatrix} . & E_A = 82.495 \\ & E_B = 81.46 \end{bmatrix}$
 $h_L = E_A - E_B$

As E_A is more than E_B and hence flow is taking Place from A to B.

Result ;

(i) Loss of head (hL) = 1.085 m. (ii) Direction of flows = From A to B.

3(b) Determine the Viscous drag torque & power absorbed on one surface of a collar bearing of 0.2 m ID & 0.3 m OD with an oil film thickness of Imm & a Viscosity of 30 centipoise if it solutes at 500. T.p.m. (6) [Nov [DEC - 2014] Given :

$$D_{i} = 0.2 m$$

 $D_{0} = 0.3 m$
 $dy = 1 mm$.
 $M = 30 C.P = 0.03 N^{4}/m^{2}$.
 $N = 500 r.p.m$.

Find :

Formula:

$$T = F \times D/2$$

folution:

(i) Velocity
$$u = \frac{\pi d; N}{60}$$

= $\frac{\pi \times 0.2 \times 500}{60}$
= $5.23 m/s$.

du = u-o ; du = 5.23 m/s.

(i) Sheart Stress
$$T = M \cdot \frac{du}{dy}$$
 [:: $T = F/A$
= 0.03 x $\frac{5.23}{0.001}$.
 $T = 156.9 N/mm^2$]

(iii) Area cy contact = 291 × T × (. [::] = 0.3-0.2
= 2TI ×
$$\begin{pmatrix} 0.8 \\ 2 & 0.05 \end{pmatrix}$$
 × 0.05 · 0.05 m]
[Area (A) = 0.0314 m²]
(iv) Force = Shear Stress (2) × Area (A)
(F) = 156.9 × 0.0314
 $\int F = 4.92 \times 0.0314$
 $\int F = 4.92 \times 0.0314$
 $\int F = 4.92 \times 0.0314$
(v) Drag Torque (T) = F × $\frac{D1}{2}$.
 $= 4.92 \times \left(\frac{0.2}{2}\right)$
Drag Torque (T) = 0.492 N-M.
Result :
Nelocity (u) = 5.25 m/s
Shear Stress (2) = 156.9 N/mm²
Area of contact (A) = 0.0314 m²
Force (F) = 4.92 N-M.
Drag Torque (T) = 0.492 N-M.

- 4. A Pipeline of 175 mm diameter beanches into two types Which delivers the water at atmospheric pressure. The diameter of branch 1 which is at 35° counter clockwise to the pipe anis is 75mm & velocity at outlet is 15m/s. The branch 2 is at 15° with the pipe center line in the Clockwise direction has a diameter of 100mm. The outlet Velocity is 15m/s. The pipes lie in a horizontal plane Determine the magnitude is direction of forces on the pipes. (16) L Nov/ DEC - 2011].
 - Given:
 - Dia, of Hain pipe (d) = 175mm = 0,175m. Dia of branch pipe 1 (d1) = 75mm = 0.75m. Velocity of branch pipe 1 (V1) = 15m/s. Dia, of branch pipe 2 (d2) = 100mm = 0.1m. Velocity of branch pipe 2 (V2) = 15m/s.

Find :

Determine magnitude 28 direction of forces.

Formula;

$$F_{R} = \sqrt{F_{m}^{2} + F_{y}^{2}}$$

$$tan \phi = \frac{F_{y}}{F_{m}}$$

Solution:

V1 = 15 mls d1 = 0.75 d = 0.175 43:01 By Continuity equation, $Q = Q_1 + Q_2$ ["Q= A × V] Av = AIVI + AaVa. $\mathcal{A} = \pi/4 d^2.$ $\frac{\overline{\Pi}}{H} d^2 \times V = \underline{\overline{\Pi}} d_1^2 \times V_1 + \underline{\overline{\Pi}} d_2^2 \times V_2.$ $\frac{\Pi}{4} \times 0.145^{2} \times V = \frac{\Pi}{4} \times 0.45^{2} \times 15 + \frac{\Pi}{4} \times 0.1^{2} \times 15.$ V = 7.65 m/s By sucrolving forces in x. direction, $F_n = F \cos \Theta + F_1 \cos \Theta_1 + F_2 \cos (360 - \Theta_2) \rightarrow \mathbb{O}$ We know that, Forme = Mar × acceleration. Mass of water (M) = PAV. -> 2

Subscritting @ In equ. @ Fn = PAN2 COSO + PA, Y12 COA 01 + PAR V22 COS (360 - 02) = (000 × T × (0.175)2 × 7.65 CO10 $F_{\rm R} = 1000 \times \frac{\pi}{4} \times 0.075^2 \times 15\cos 35^\circ$

$$= (000 \times \frac{\pi}{4} \times 0.1^{2} \times 15 (0s (360 - 15^{\circ})),$$

$$F_{n} = 352.08 \text{ N}.$$
Provide the form of the effective of the effe

The discution of substant force x. and, $\tan 0 = \frac{F_y}{F_n}$ $= \frac{7.52}{352.08} \Rightarrow 0.0214$

Rerult :

5. A pipe 200m long stopes down at 1 in 100. and tapers from 600mm diameter at the lower end, and carrier 100 lit / sec of oil having specific gravity 0.8. If the pressure gauge at the higher end seads 60 KN/m². If the pressure gauge at the higher end seads 60 KN/m². determine the velocities at the two end. also the pressure at the lower end. Neglect all losses. (16) [Apr/may-2015] Given:

$$L = 200 \text{ m.}$$

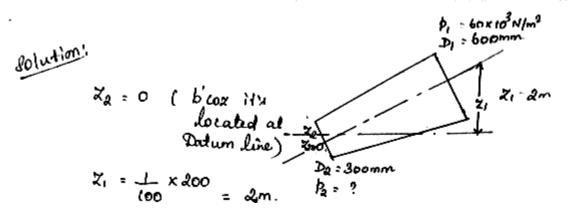
Stopes at = 1/100.
 $\dot{D}_1 = 600 \text{ mm.}$
 $D_2 = 300 \text{ mm.}$
 $Q = 100 \text{ Lit / sec} = 0.1 \text{ m}^3/\text{s.}$
 $P_1 = 60 \times 10^3 \text{ N/m}^2$; $S = 0.8$.

Find :

pressure at the lower end (Pr) = ?

formula required: Apply beenoulli's equation.

$$\frac{P_{1}}{P_{g}} + \frac{V_{1}^{2}}{2g} + Z_{1} = \frac{P_{g}}{P_{g}} + \frac{V_{a}^{2}}{2g} + Z_{a}$$



$$\begin{aligned} & \mathcal{Q} = A_{1} V_{1} = A_{2} V_{2}. \\ & \mathcal{Q} = A_{1} V_{1} \\ & \mathcal{O}_{1} = \frac{T}{H} (d_{1})^{2} \times V_{1} ; \frac{T}{H} \times (0.6)^{2} \times V_{1} \\ & V_{1} = \frac{0.1}{\frac{T}{H} (0.6)^{2}} \Rightarrow \frac{0.1}{0.2824} \Rightarrow 0.353 \text{ m/s} \\ & \boxed{V_{1} = 0.353 \text{ m/s}} \\ & \boxed{V_{1} = 0.353 \text{ m/s}} \\ & \mathcal{Q} = A_{2} V_{2}. \\ & \mathcal{O}_{1} = \frac{T}{H} (d_{2})^{2} \times V_{2} : \frac{T}{H} \times (0.3)^{2} \times V_{2}. \\ & V_{q} = \frac{0.1}{\frac{T}{H} (0.3)^{2}} \Rightarrow \frac{0.1}{0.0706} \Rightarrow 1.4164 \text{ m/s}. \\ & V_{q} = \frac{1.4164 \text{ m/s}}{\frac{T}{H} (0.3)^{2}} \Rightarrow \frac{1.4164 \text{ m/s}}{2g} + X_{q}. \\ & \frac{b_{1}}{P_{q}} + \frac{V_{1}^{2}}{2g} + X_{1} = \frac{b_{2}}{P_{q}} + \frac{V_{2}^{2}}{2g} + X_{q}. \\ & \frac{b0 \times 10^{3}}{(000 \times 9.8)} + \frac{(0.353)^{2}}{2 \times 9.81} + 2 = \frac{b_{2}}{P_{q}} + \frac{(1.416)^{2}}{2 \times 9.81} + 0 \end{aligned}$$

$$b_{111b} + \frac{0.124b}{19.62} + 2 = \frac{b_2}{pg} + \frac{2.005}{19.62} + 0$$

$$b_{11b} + b_{135} \times 10^{-3} + 2 = \frac{b_2}{pg} + 0.102 + 0.$$

$$p_{g}$$

$$b_{12} = \frac{b_2}{pg} + 0.102 + 0$$

$$\frac{b_2}{pg} = 8.12 - 0.102$$

$$\frac{b_2}{pg} = 8.018 \times P \times g.$$

$$= 8.018 \times 1000 \times 9.81$$

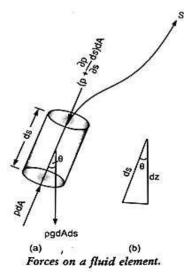
$$= 786556.58 \text{ N/m^2} (0x)$$

$$= 78.65 \text{ KN/m^2}$$

Remult :
premule at the lawer end $(b_2) = 78.65 \text{ KN/m^2}.$

ŝ

6. Derive the Bernoulli's equation from Euler's Equation. (Nov/Dec 2015)



This is equation of motion in which the forces due to gravity and pressure are taken into consideration. This is derived by considering the motion of a fluid element along a stream line as

- 1. Pressure force pdA in the direction of low
- 2. Pressure force ds dA opposite to the direction of flow $\{p+\frac{6p}{6s}\}$
- 3. Weight of element ρ gdAds

If

Let θ is the angle between the direction of flow and the line of action of the weight of element.

The resultant force on the fluid element in the direction of s must be equal to the mass of fluid element X acceleration in the direction s.

$$pdA - \{p + \frac{\phi}{6s} ds\} dA - \rho g dAds \cos \theta$$
$$= \rho dAds X a_s \dots 1$$

Whereas is the acceleration in the direction of s

$$a_{s} = \frac{dv}{dt} \text{ where } v \text{ is a function of s and t.}$$
$$= \frac{6v}{6s}\frac{ds}{dt} + \frac{6v}{6t}$$
$$= v\frac{6v}{6s} + \frac{6v}{6t} \qquad \{v = \frac{ds}{dt}\}$$
the flow is steady, $\frac{dv}{dt} = 0$
$$a_{s} = v\frac{6v}{6s}$$

Substituting the value of a_l in equation 1 and simplifying the equation, we get

$$\frac{-6p}{6s} ds - \rho \text{gdAds } \cos \theta = \rho \text{dAds } x \frac{6v}{6s}$$

Dividing by ρdAds , $\frac{-6p}{\rho 6s} - g \cos \theta = v \frac{6v}{6s}$
 $\frac{6p}{\rho 6s} + g \cos \theta + v \frac{6v}{6s} = 0$
From fig $\cos \theta = \frac{dz}{ds}$

$$\frac{1}{\rho}\frac{dp}{ds} + g\frac{dz}{ds} + v\frac{dv}{ds} = 0$$
$$\frac{dp}{\rho} + g dz + v dv = 0$$

This equation is known as Euler's equation of motion

BERNOULLI' S EQUATION FROM EULER'S EQUATION

Bernoulli's equation is obtained by integrating the Euler's equation of motion

$$\int \frac{dp}{\rho} + \int g \, dz + \int v \, dv = \text{constant} - 2$$

$$\frac{p}{\rho} + g \, z + \frac{v^2}{2} = \text{constant}$$

$$\frac{p}{\rho g} + z + \frac{v^2}{2g} = \text{constant}$$

$$\frac{p}{\rho g} = \text{pressure energy per unit weight of fluid pressure head}$$

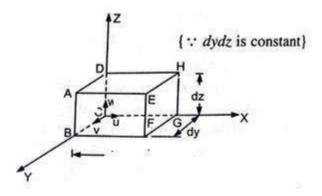
$$\frac{v^2}{2g} = \text{kinetic energy per unit weight or kinetic head}$$

$$Z = \text{potential energy per unit weight or potential head}$$

Equation 2 is called Bernoulli's equation.

7. Derive the continuity equation for three dimensional flow of a fluid with neat skeatch. (April/May 2011)

CONTINUITY EQUATION IN THREE-DIMENSIONS



Consider a fluid element of lengths dx, dy and dz in the direction of x, y and z. Let u, v and w are the inlet velocity components in x, y and z directions respectively. Mass of fluid entering the face ABCD per second

 $= \rho \times \text{Velocity in x-direction} \times \text{Area of ABCD}$ $= \rho \times \upsilon \times (\text{dy} \times \text{dz})$ Then mass of fluid leaving the face EFGH per second $= \rho \upsilon \qquad ^{6} \partial \textbf{u} \text{ dy dz}) \text{ dx}$ $\text{dydz}_{\overline{6x}}($ $\therefore \text{ Gain of mass in X-direction}$ = Mass through ABCD-Mass through EFGH per sec $= \rho \textbf{u} \text{ dy dz} - \rho \textbf{u} \text{ dydz} - \frac{6}{6x}(\partial \textbf{u} \text{ dy dz}) \text{ dx}$

$$=-\frac{6}{6x}(\rho u dydz) dx$$

 $=-\frac{6}{6x}(\rho u)dx dydz$

Similarly, the net gain of mass in Y-direction

=-
$$\frac{6}{6y}$$
(pv) dxdydz

and in Z-direction $=-\frac{6}{6z}(\rho w)dxdydz$

 $\therefore \text{ Net gain of masses}=-\left[\frac{6}{6x}(\rho u)_{+}\frac{6}{6y}(\rho v)+\frac{6}{6z}(\rho w)\right] dxdydz$

Since the mass is neither created nor destroyed in the fluid element, the net increase of mass per unit time in the fluid element must be equal to the rate of increase of mass of fluid in the element.

But mass of fluid in the element is ρ . dx.dy.dz and its rate of increase with time

Equating the two expressions $is^{\frac{6}{}}(\rho dx.dy.dz)$ or dx dy dz. Equation (1) is the continuity equation in Cartesian co-ordinates in its most general form. This Equation is applicable to:

- (i) Steady and unsteady flow,
- (ii) Uniform and non -uniform flow, and
- (iii) Compressible and incompressible fluids.

For steady flow, $\frac{\beta}{6t} = 0$ and hence equation (1) becomes as

$$\frac{6}{6x}(\rho u)_{+\frac{6}{6y}}(\rho v) + \frac{6}{6z}(\rho w) = 0$$

If the fluids is incompressible, then p is constant and the above equation becomes as

$$\frac{6u}{6x} + \frac{6v}{6y} + \frac{6w}{6z} = 0$$

9 calculate the dynamic viscosity of the oil which is used for lubrication between a square plate of 0.8m×0.8m, and an inclined plane with an angle of inclination 30°, as shown in the big The weight of the square plate is 300 N and its slides down the inclined plan with a uniform velocity of 0.3 m/s. The thickness of oil film is 1.5 mm. given: W sin 30°- F=0 F 20 00 30 F = WAIN 30° y=1.5mm to whinze = Wg = 300 shear force, F = 150 N.] * purpose area of square plate, a = 0 8m x0.8m = 0.64 m2. * Angle of chilination , $0 = 30^{\circ}$ * weight of plate w = 300N* rangential velocity of the plate, u=0.3mls * Thickness of oil film, y = 1. 5 mm

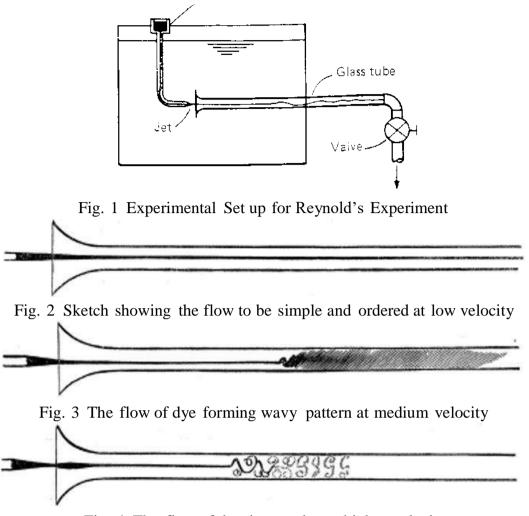
=1.5 ×10 m

find μ : Recolving the forme F_1 whin 30° - F = 0 $F = \omega \sin 30^{\circ}$ F=300 × 10 Mean forme, F=150 N * shear stress, T = E a = 150 0.64 F = 234. 875 N/m2. * Dynamic vie cosity, $\mu = \tau \times dy$ du = 234.375× 1.5×10-3 pc = 1. 171875 Ns(m2 1 = 11.718 Poise . [: 1 Poise - [Nsim] Result: Dynamic viscosity of oil = 11.718 Poise.

PART C

1. Explain Reynold's experiment. (Nov/Dec 2016)

In 1880's, Professor Osborne Reynolds carried out numerous experiment on fluid flow. We will now discuss the laboratory set up of his experiment. The experimental set used by Prof. Osborne Reynold is shown in Fig 1. As you can see from the figure, Reynolds injected dye jet in a glass tube which is submerged in the large water tank. Please see that the other end of the glass tube is out of water tank and is fitted with a valve. He made use of the valve to regulate the flow of water. The observations made by Reynolds from his experiment are given shown through Figures 5 to 7.



Dye

Fig. 4 The flow of dye is complex at higher velocity

APPROACH TOWARDS REYNOLDS' NUMBER

Throughout the experiment, Reynolds thought that the flow must be governed by a dimensionless quantity. What he observed was that Inertial force/Viscous force is unit less (dimensionless). Let us see the mathematical expression of inertial force and viscous force.

Inertial force is the force due to motion i.e. which may be also called as kinetic force.

```
Kinetic energy = \frac{1}{2} \text{ mv}^2
Inertia force = \rho v^2/2
Viscous force = \mu (du/dy)
Reynold's Number = Inertia force/ Viscous force
= \rho v^2 dy/\mu du
```

Now, for a finite length we can write dy = l, and du = v Reynold's Number = Inertia force/ Viscous force

$$= \rho v^2 l/\mu v$$

Reynold's number = ρ **.v.l**/ μ

2. The dynamic Viscosity of an oil used for
lubrication between a shaft and sleave is 6 poise.
The shaft is of diameter 0.4 m and Rotates at
190 rpm. Calculate the power lost in the bearing.
for a sleave length of 90 mm. The thickness of the
oil film is 1.5 mm.
Power =
$$\frac{2\pi NT}{60}$$
 = 716.48 w
T = Force $\times \frac{9}{2}$ = 36.01 Nm
Force = Shear stress \times Area
= $1592 \times \pi DL$
shear stress, $T = \int \frac{du}{dy} = 1592 \cdot N[m^2]$
 $du = u - 0 = 2.98 m/s$
Tangutial Velvoety, $u = \frac{\pi DN}{60} = 3.98 m/s$

UNIT –II

FLOW THROUGH PIPES AND BOUNDARY LAYER

1. Difference between hydraulic Gradient line and Energy Gradient line. (Nov/Dec 2015, May/June 14,09)

Hydraulic gradient line :-

Hydraulic gradient line is defined as the line which gives the sum of pressure head and datum head of a flowing fluid in a pipe with respect the reference line

Total energy line :-

Total energy line is defined as the line which gives the sum of pressure head , datum head and kinetic head of a flowing fluid in a pipe with respect to some reference line

2. Mention the general characteristics of laminar flow. (May/june 14)

- 1. There is a shear stress between fluid layers
- 2. 'No slip' at the boundary
- 3. The flow is rotational
- 4. There is a continuous dissipation of energy due to viscous shear

3. Define boundary layer thickness (Nov/Dec 15)

It is defined as the distance from the solid boundary in the direction perpendicular to the direction of flow where the velocity of fluid is approximately equal to 0.99 times the free stream velocity

4. What is Hagen poiseuille's formula ? (May/june12,Nov/Dec 2012)

P1-P2 / pg = h f = 32 μ UL / _gD²

The expression is known as Hagen poiseuille formula .

Where P1-P2 / $_g$ = Loss of pressure head U = Average velocity

 μ = Coefficient of viscosity D = Diameter of pipe

L = Length of pipe

5. What is the expression for head loss due to friction in Darcy formula?

(Nov/Dec 2010)

$$hf = 4fLV^2 / 2gD$$

Where f = Coefficient of friction in pipe L = Length of the pipe D = Diameter of pipe V = velocity of the fluid

6. List the minor energy losses in pipes? (Nov/Dec 2010,May/June 07)

This is due to

- i. Sudden expansion in pipe ii. Sudden contraction in pipe .
- iii. Bend in pipe . iv. Due to obstruction in pipe

7. What are the factors influencing the frictional loss in pipe flow?

Frictional resistance for the turbulent flow is

- 1. Proportional to vn where v varies from 1.5 to 2.0 .
- 2. Proportional to the density of fluid .
- 3. Proportional to the area of surface in contact .
- 4. Independent of pressure . Depend on the nature of the surface in contact.

8. What are the basic educations to solve the problems in flow through branched pipes?

- i. Continuity equation .
- ii. Bernoulli's formula .
- iii. Darcy weisbach equation .

9. What is Dupuit's equation ?

$$(L_1/d_1^5)+(L_2/d_2^5)+(L_3/d_3^5)=(L / d^5)$$

Where

L1, d1 = Length and diameter of the pipe 1

L2, d2 = Length and diameter of the pipe 2

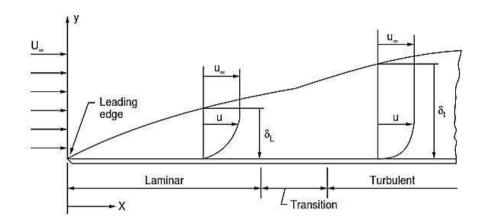
L3, d3 = Length and diameter of the pipe 3

10. Define Moody diagram (Nov/Dec 2012, April/May 11)

It is a graph in non-dimensional form that relates the Darcy friction factor, Reynolds number and relative roughness for fully developed flow in a circular pipe.

11. Define boundary layer. (April/May 2017)

When fluids flow over surfaces, the molecules near the surface are brought to rest due to the viscosity of the fluid. The adjacent layers also slow down, but to a lower and lower extent. This slowing down is found limited to a thin layer near the surface. The fluid beyond this layer is not



affected by the presence of the surface. The fluid layer near the surface in which there is a general slowing down is defined as boundary layer.

12. What are equivalent pipes? Mention the equation used for it. (April/May 2017)

Equivalent pipes are defined as the pipes of uniform diameter having loss of head and discharge equal to the loss of head and discharge of a compound pipe consisting of several pipes of different lengths and diameters. The uniform diameter of the equivalent pipe is called equivalent size of the pipe.

The equation used to represent equivalent pipe is called Dupit's equation which is given as,

$$(L_1/d_1^5)$$
+ (L_2/d_2^5) + (L_3/d_3^5) = (L/d^5)

Where

L1, d1 = Length and diameter of the pipe 1

L2, d2 = Length and diameter of the pipe 2

L3, d3 = Length and diameter of the pipe 3

1. A laminar flow is taking place in a pipe at dia 20cm. The mominum velocity 1.5 m/s. Find near velocity and radius at which this occurs. Also. Calculate Velocity at 4 cm from wall of pipe. (16) [NOV/Dec-2013]

Given: D = 20 cm. = 0,20 m. Uman = 1.5 m/s.

Find : (1) mean velocity, T. (2) Radius at which To occurs. (12) Velocity at Acm from the wall.

Solution:
(i) Ratio of
$$\frac{Uman}{U} = 2.0$$
 [Taken from
the Decivation]
 $\frac{1.5}{U} \pm 2$
 $\overline{u} = \frac{1.5}{2} = 0.75 \text{ m/s}$
(i) Radius at which \overline{u} occurs.
(i) Radius at which \overline{u} occurs.
The velocity u , at any radius 'r, 's givenby
 $u = (-\frac{y_{HM}}{2}) [R^2 - r^2] (0r)$
 $u = (-\frac{y_{HM}}{2}) R^2 [1 - \frac{\gamma^2}{R^2}]$

Bud from equation
$$\mathcal{O}_{man}$$
 is given by

$$\mathcal{O}_{man} = -\frac{1}{4u} \left(\frac{\partial p}{\partial n}\right) \cdot \mathbb{R}^{q}.$$

$$\begin{bmatrix} \vdots & u = \mathcal{O}_{man} \left[1 - \left(\frac{r}{R}\right)^{q} \right] \\ \text{Nowo, the radiusivat which $u = \overline{u} = 0.75 \text{ m/s}.$

$$0.75 = 1.5 \int \left[1 - \left(\frac{r}{\mathcal{O} \cdot 2/2}\right)^{2} \right] \\ = 1.5 \int \left[1 - \left(\frac{r}{\mathcal{O} \cdot 2/2}\right)^{2} \right] \\ = 1.5 \int \left[1 - \left(\frac{r}{\mathcal{O} \cdot 1}\right)^{2} \right] \\ \frac{0.75}{10.5} = 1 - \left(\frac{r}{\mathcal{O} \cdot 1}\right)^{2} \\ \frac{r}{\mathcal{O} \cdot 1} = 1 - \frac{0.75}{0.1 + 5} = 1 - \frac{1}{2} = \frac{1}{2} \\ \text{Y} = 0.11 \times \sqrt{0.5} \\ = 0.1 \times \sqrt{0.5} \\ = 0.1 \times \sqrt{0.75} = 0.0707 \text{ m}.$$

$$\left[\frac{r}{r} = \frac{7}{40.7 \text{ mm}} \right] \\ (\text{w}) \text{ Velocity at Acm from the wall,} \\ r = R - 4.0 \\ = 10 - 4 \Rightarrow 6.cm (0.5) 0.06 \text{ m}. \end{cases}$$$$

The velocity at a radius = 0.06 m (b)
A cm grow pipe wall
$$u$$
 given by
= $0 \text{man} \int (1 - (T/R)^2)^2$
= $1.5 \int (1 - (0.06)^2)^2$
= $1.5 \int (1 - (0.06)^2)^2$
= $1.5 \int (1.0 - 0.36)^2$
= $1.5 \times 0.64 = 0.96 \text{ m/s}$.

Reput :

Mean Velocity II: 0,75 m/s. radius at which (x) = 70,7 mm. To occurs (x) = 70,7 mm. Velocity at 4 cm from (u) = 0,96 m/s. the wall.

2. An oil of specific gravity 0,80 & Kinematic Vircority 15 x 10⁻⁶ m²/s. flows in a Smooth pipe of 12 cm diameter at a sate of 150 lit/min. Determine whether the flow is laminar or turbulint. Also calculate the velocity at the center line & velocity at a radius of 4 cm. What a head loss for a length of com? What will be the entry length? Also determine the wall shear (16) [Nov 1De.

Griven:

$$g = 0.80$$
.
 $g = 1.5 \ 15 \ x to^{-6} m^2/s$.
 $d = 0.12 m$.
 $d = 0.12 m$.
 $G = 150 \ 1/min = \frac{15 \times 10^{-3}}{60} = 0.0025 \ m^3/s$
 $T = 4 \ cm = 0.04 m$.

(ng-ni) dn = 10m.

Find :

Solution:

(i)
$$Re = \frac{VD}{V}$$

$$Q = A \times V$$

 $V = Q A$

$$V = , \frac{0.0025}{T/\psi (0.12)^{2}}$$

$$R_{e} = \frac{0.221 \text{ m/s}}{15 \times 10^{-6}} \Rightarrow 1768.3$$

$$R_{e} < 2000 ; ..., The flow is laminar.$$
(6) $U_{man} = \frac{1}{4\pi (\frac{\partial p}{\partial n}) \cdot R^{q}}$

$$P_{i} - P_{a} = \frac{32\mu\overline{u}L}{D^{2}} \qquad \frac{\partial p}{\partial n} = \frac{P_{a} - P_{i}}{Z_{g} - Z_{1}}$$

$$\overline{u} = V = 0.221 \text{ m/s}$$

$$P_{i} - P_{a} = \frac{32\mu\overline{u}L}{D^{2}} \qquad \frac{\partial p}{\partial n} = \frac{V_{a} - P_{i}}{Z_{g} - Z_{1}}$$

$$\overline{u} = V = 0.221 \text{ m/s}$$

$$P_{i} - P_{a} = \frac{32 \times 0.012 \times 0.221 \times 10}{(0.12)^{2}} \qquad \text{m} = 32.555\%$$

$$P_{i} - P_{a} = 58.946 \text{ N/m}^{2}. \qquad P_{a} = 1000 \times 0.8$$

$$U_{man} = \frac{1}{4\pi 0.012} \times \frac{58.944}{10} \times 0.06^{2} = 800 \text{ kg/m}^{3}$$

$$U_{man} = 0.441 \text{ m/s}$$

(iii) Velocity at 4 cm from center.

$$T = 0.04 \text{ m.}$$

$$= 0.441 \left(1 - (7/R)^{2} \right)$$

$$= 0.245' \text{ m/s}.$$
(i) voall shear.

$$T_{0} = - \left(\frac{\partial p}{\partial m}\right) \times \binom{R/2}{2}$$

$$= \frac{p_{1} - p_{2}}{Z} \times \binom{R/2}{2}$$

$$= \frac{58.94}{K} \times \frac{0.06}{2}$$

$$T_{0} = 0.1767 \text{ N/m}^{2}.$$
N) Head loss for largth tom.

$$h_{4} = \frac{82 \text{ MTL}}{R_{0} \times 9.61 \times (0.12)^{2}}$$

$$h_{4} = 0.0075 \text{ m}$$

Reput : (i) hf = 0,0075m (1) wall shear (20) = 0.1767 N/m2. (eii) The velocity at 1 = 0.245 m/s. 4 cm from center = 0.245 m/s.

Oil flows through a pipe 150 mm in diameter and 650 mm in length with a velocity of 0.5 m/s. If the Kinematic Viscosity of 0il is 18,7 × 10 - 4 m²/s. Find the power lost in over coming friction. Take Sp. g. of 0il as 0.9. (16) [APr/may - 2015]

Given: d = 150mm = 0.15 L = 650mm = 0.65 V = 0.5mls $V = 18.7 \times 10^{-4} m^{2}/s$ S = 0.9 $[:P = 0.9 \times 1000$ $= 900 \text{ kg/m^{3}}$

3.

Find: Power lost (P)

Formula: $p = \frac{P B g h f}{1000} K W.$

Solution:

$$R_{e} = \frac{\sqrt{D}}{\sqrt{2}}$$

$$= \frac{0.5 \times 0.15}{18.7 \times 10^{-4}} \Rightarrow \frac{0.075}{18.7 \times 10^{-4}}$$

$$R_{e} = 40.106 < 2000. \quad f \quad R_{e} \quad Value is$$

$$R_{e} = 461 \sqrt{2}$$

$$29 \times d.$$

$$f = \frac{16}{R_{e}}$$

$$= \frac{16}{40.106}$$

$$f = 0.3$$

$$h_{f} = \frac{14 \times 0.3 \times 650 \times (0.5)^{2}}{0.15 \times 2 \times 9.81}$$

$$h_{f} = \frac{195}{2.943} \Rightarrow 66.25$$

$$\boxed{h_{f}} = \frac{195}{2.943} \Rightarrow 66.25$$

$$= \frac{9.81 \times 1900 \times 0.0088 \times 66.25}{1000}$$

$$P = 5.147 \times 1000$$

4. Two pipes of dia 40cm & 20 cm are each 300m long. when pipes connected in Series & 0.10 m3/s. Find loss of head & loss of head in S/m to pass the same total discharge when pipes connected in parallel Take f: 0.0075 for each pipe (16) [Nov/Dec - 2010]

Gliven:

$$D_1 = 40 \text{ cm} = 0.4 \text{ m}.$$

 $D_2 = 20 \text{ cm} = 0.2 \text{ m}.$
 $L_1 = L_2 = 300 \text{ m}.$
 $Q = 0.1 \text{ m}^3/s.$
 $f = 0.0075.$

Find : (i) head loss for series & parallel.

Solution:

For series connection,

$$Q = A_1 V_1 = A_2 V_2$$

$$Q = A_1 V_1$$

$$Q_2 = A_2 V_2$$

$$Q_1 = \frac{TT}{4} (0.4)^2 \times V_1$$

$$V_1 = 0.79 \text{ m/s}$$

$$V_2 = 3.18 \text{ m/s}$$

Neglecting the minox losses.

$$H = \frac{4fL_{1}V_{1}^{2}}{2gd_{1}} + \frac{4fL_{2}V_{2}^{2}}{2gd_{2}}.$$

$$= \frac{4 \times 0.0075 \times 300 \times (0.74)^{2}}{2 \times 9.81 \times 0.4}$$

$$= \frac{4 \times 0.0075 \times 300 \times (3.18)^{2}}{2 \times 9.81 \times 0.2}$$

$$H = 0.715 + 23.19$$

$$H = 23.4 \text{ m}$$
Fox parallel connection,

$$h_{f} = \frac{4fL_{1}V_{1}^{2}}{2g \times d_{1}} = \frac{4fL_{2}V_{2}^{2}}{2g \times d_{2}}$$

$$\frac{V_{1}^{2}}{D_{1}} = \frac{V_{2}^{2}}{D_{2}}$$

$$\frac{V_{1}^{2}}{0.4} = \frac{V_{2}^{2}}{0.2}$$

$$V_{1} = 1.41.V_{2}$$

$$Q = A_{1}V_{1}$$

$$O_{1}(2 \times V_{1}) = 1.41.V_{2}$$

$$Q = A_{1}V_{1}$$

$$V_{1} = 0.749 \text{ m/s}$$

$$Q = A_1 V_1 = A_2 V_2.$$

$$Q = A_2 V_2$$

$$V_2 = 0.56 \text{ m/s}$$

$$h_f = \frac{4f \lambda_1 V_1^2}{29 \text{ xd},}$$

$$z = \frac{4 \times 0.0075 \times 300 \times (0.79)^2}{2 \times 9.81 \times 0.4}$$

$$h_f = 0.71 \text{ m/s}$$

Result ; Head Loss for Series pipe is 0.71 m. Head Loss for parallel pipe is 0.71 m.

5. A pipe line of 0.6 m dianeter is 1.5 Km long. TO Increase the discharge, another line of the Same dianeter is Introduced Parallel to the flyst in the Second half of the length. Neglecting minory Cosses. find the Increase in discharge if Af=0.04. The head at Inlet is 300mm. [16] [Apr/may-2015]

$$f = 0.01$$
Head at Jn/et $h = 300mm = 0.3m$
Head at outlet $= atmaspheric head = 0$

i. blead loss $(h_f) = 0.3m$

length of another facallel fipe $L_1 = \frac{1500}{2}$

 $= 750m$.

Dia of another facallel pipe. $d_1 = 0.6m$.

 $\frac{1 = 1500m}{4} = \frac{L = 1500m}{2} = \frac{L = 30m}{2}$.

 $\frac{L = 1500m}{2} = \frac{L = 30m}{2}$.

 $\frac{L = 1500m}{2} = \frac{L = 30m}{2}$.

2nd case.

When an additional pipe of length 750m is diameter 0.6 m is connected in parallel with the last half length of the pipe. 1 st parallel pipe. Let, $Q_1 \rightarrow discharge in$ By > discharge in 2rd parallel pipe $Q = Q_1 + Q_2$. where, $Q \rightarrow discharge in mainpipe when pipes are multiple in the pipe of the second s$ parallel. But as the length is diameters of each parallel pipe is sane $Q_1 = Q_2 = Q/2$ Consider the flow through pipe ABC on ABD Head loss through ABC = Head lost + Headlost -> 0 int head last due to friction through ABC = 0.3 m given. $\frac{1}{9} \log due to$ $\frac{1}{9} \log due$ $\frac{1}{9} \log due to$ $\frac{1}{9} \log due$ $\frac{1}{9} \log due$ $\frac{1}{9} \log due$ $\frac{1}{9} \log due$ $\frac{1}{9}$ blead loss due to Where V = Velocity of = $\frac{Q}{Area}$, $\frac{Q}{\overline{\pi}/4(0.6)^2}$ = $\frac{40}{\overline{\pi}\times0.36}$ How the only AB . Head loss due to friction through AB $= \frac{4 \times 0.01 \times 750}{0.6 \times 2 \times 9.81} \times \left(\frac{40}{11 \times 0.36}\right)^{2}$ = 31,87Q²

Head loss due to friction through BC

$$= \frac{4 \times f \times h}{x \times y}^{2}$$

$$= \frac{4 \times 0.01 \times 750}{0.6 \times 2 \times 9.81} \propto \left[\frac{Q}{2 \times 17/y}(0.6)^{2}\right]$$

$$= \frac{4 \times 0.01 \times 750}{0.6 \times 2 \times 9.81} \propto \left[\frac{(..., V_{1} = Disclarge(Q))}{A \times 10^{2}}\right]$$

$$= \frac{4 \times 0.01 \times 750}{0.6 \times 2 \times 9.81} \times \frac{16}{4 \times 10^{2} \times 0.36^{2}} = \frac{Q}{17/4} (0.6)^{2}$$

$$= \frac{7.969}{9.839} Q^{2}$$
Substituting these values in equ (1) we get,

$$0.3 = 31.87 Q^{2} + 7.969 Q^{2}$$

$$= 39.839 Q^{2}$$

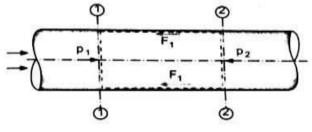
$$Q = \sqrt{\frac{0.3}{39.839}} = 0.0867 \text{ m}^{3}/s.$$

$$\therefore \text{ Increase in discharge} = Q - Q^{4}$$

$$= 0.0867 - 0.0685$$

$$= 0.0182 \text{ m}^{3}/s.$$

6. Derive the Darcy-Weisbach equation for calculating pressure drop in pipe. (Nov/Dec 2011)



Uniform borizontal pipe.

Consider a uniform horizontal pipe, having steady low as shown figure let 1-1 and 2-2 are two sections of pipe

 P_1 = pressure intensity at section 1-1

 V_1 = velocity of flow at section 1-1

L = length of the pipe between sections 1-1 and 2-2

D = Diameter of pipe

F = Frictional resistance per unit wetted area per unit velocity

 h_f = loss of head due to friction

 $P_2 \,and \, V_2 \,are \,values \,of \, pressure \,$ intensity and velocity at section 2-2

Applying Bernoulli's equation between sections 1-1 and 2-2,

Total head at 1-1 = total head at 2-2 + loss of head due to friction between 1-1 and 2-2

$$\frac{p_1}{\rho_g} + \frac{v_1^2}{2g} + z_1 = -\frac{p_2}{\rho_g} + \frac{v_2^2}{2g} + z_2 + h_f$$

z₁= z₂as pipe is horizontal

 $v_1 = v_2$ as dia of pipe is same at 1-1 and 2-2

But h_f is the head lost due to friction and hence intensity of pressure will be reduced in the direction of row by frictional resistance

Now frictional resistance = frictional resistance per unit wetted area per unit velocity X wetted area X velocity²

$$F_1 = f X \pi dLX V^2 \qquad \{ \text{Wetted area} = , \quad V = V_1 = V_2, \text{ Perimeter } P = \pi d \}$$
$$F_1 = f P L V^2$$

The forces acting on the fluid between sections 1-1 and 2-2 are

- > Pressure force at section $1-1 = p_1 A$
 - Where A = Area of pipe
- > Pressure force at section $2-2 = p_2 A$
- ➢ Frictional force F₁

Resolving all Forces in the horizontal direction, we have

$$p_1 A - p_2 A - F_1 = 0$$

($p_1 - p_2$) $A = F_1 = f P L V^2$

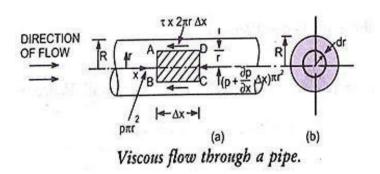
But from equation $1(p_1 - p_2) = \rho g h_f$

Equating the value of $(p_1 - p_2)$ we get h_f = 4flv²/2gd

FLOW OF VISCOUS FLUID THROUGH CIRCULAR PIPE

For the flow of viscous fluid through circular pipe, the velocity distribution across a section The ratio of maximum velocity to average velocity, the shear stress distribution and drop of Pressure or a given length is to be determined. The flow through the circular pipe will be viscous Or laminar, if the Reynolds number (R_e) is less than 2000.The expression for Reynolds number is given by

$$R_e = \frac{\rho VI}{\mu}$$



 ρ =Density of fluid flowing through pipe V=Average velocity of fluid D=Diameter of pipe and μ =Viscosity of fluid

Consider the horizontal pipe of radius R. The viscous fluid is flowing from left to right in the pipe as Shown in fig. consider a fluid n element of radius r, sliding in a cylindrical fluid element of radius

1. Shear stress distribution

(r+dr).Let the length of fluid element be Δx . If 'p' is the intensity of pressure on the face AB,thenthe intensity of pressure on the face CD will be $(p+{}^{6p}\Delta x)$.Then the forces acting on the fluid element are

1. The pressure force, $p \times \pi r^2$ on face AB.

2. The pressure force, $(p + \frac{6p}{6x}\Delta x) \pi r^2$ on force CD.

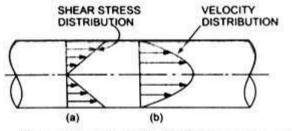
3. The shear force, $\tau \times 2\pi r \Delta x$ on the surface of fluid element .As there is no acceleration; hence the Summation of all forces of all forces in the direction of flow must be zero i.e.

$$p\pi r^{2} - (p + \frac{6p}{6x} \Delta x) \pi r^{2} - \tau \times 2\pi r \times \Delta x.=0$$
Or
$$-\frac{6p}{6x} \Delta x \pi r^{2} - \tau \times 2\pi r \times \Delta x = 0$$
Or
$$-\frac{6p}{6x} r - 2\tau = 0$$

$$\therefore \tau = -\frac{6p}{6x} \frac{r}{2} - -----(1)$$

The shear stress τ across a section varies with 'r' as $\frac{6p}{6x}$ across a section is constant.

2. Velocity Distribution.



Shear stress and velocity distribution across a section.

To obtain the velocity distribution across a section, the value of shear stress $\tau = \mu \frac{du}{dy}$ is substituted in equation (1)

But in the relation $\tau = \mu \frac{du}{dy}$, y is measured from the pipe wall. Hence Y=R-r and dy = -dr

$$\therefore \qquad \tau = \mu \frac{du}{-dr} = -\mu \frac{du}{dr}$$

Substituting this value in (1), we get

$$-\mu \frac{du}{dr} = -\frac{6p}{6x} \frac{r}{2} \text{ or } \frac{du}{dr} = \frac{1}{2\mu} \frac{6p}{6x} r$$

Integrating this above equation w.r.t. 'r', we get

$$\mu = \frac{1}{4\mu} \frac{6p}{6x} r^2 + C$$

Where C is the Constant of Integration and its value is obtained from boundary condition that at r=R, μ =0.

$$\therefore \quad 0 = \frac{1}{4\mu} \frac{6p}{6x} R^2 + C$$

$$\therefore \quad C = -\frac{1}{4\mu} \frac{6p}{6x} R^2 \qquad (2)$$

Substituting this value of C in equation

$$\mu = \frac{1}{4\mu} \frac{\overline{6p}}{6x} \overline{r^2} - \frac{1}{4\mu} \frac{6p}{6x} R^2$$

$$\therefore = -\frac{1}{4\mu} \frac{6p}{6x} [R^2 - r^2] - \dots$$
(3)

In equation (3), values of μ , $\frac{6p}{6x}$ and R are constant, which means the velocity, μ varies with the square of r. Thus equation (3) is an equation o parabola. This shows that the velocity distribution across the section of a pipe is parabolic. This velocity distribution is shown in fig.

1. Ratio of Maximum Velocity to Average Velocity.

The velocity is maximum, when r=0 in equation Thus maximum velocity, U_{max} is obtained as $U_{max} = \frac{1}{2} \frac{1}{6n} \frac{1}{2}$

$$U_{\text{max}=} - \frac{6p}{4\mu} \frac{6p}{6x} R^2 - \dots - (4)$$

The average velocity, u, is obtained by dividing the discharge of the fluid across the section by the area of the pipe (πR^2). The discharge (Q) across the section is obtained by considering the flow through a circular ring element of radius r and thickness dr as shown in Fig. The fluid flowing per second through this elementary ring

dQ = velocity at a radius r ×area of ring element

$$=u \times 2 \pi r dr$$

$$= -\frac{1}{4\pi} \frac{6p}{6x} [R^2 - r^2] \times 2 \pi r dr$$

$$Q = \int_0^{R} \frac{1}{6x} \frac{6p}{4\mu} \sum_{k=0}^{R} (R^2 - r^2) \times 2 \pi r dr$$

$$= \frac{1}{4\mu} (-\frac{6p}{6x}) \times 2 \pi \int_0^{R} (R^2 - r^2) r dr$$

$$= \frac{1}{4\mu} (-\frac{6p}{6x}) \times 2 \pi \int_0^{R} ((R^2r - r^3)) dr$$

$$= \frac{1}{4\mu} (-\frac{6p}{6x}) \times 2 \pi [\frac{R^2r^2}{2} - \frac{r^4}{4}] = \frac{1}{4\mu} (-\frac{6p}{6x}) \times 2 \pi [\frac{R^2r^2}{2} - \frac{r^4}{4}]$$

$$= \frac{1}{4\mu} (-\frac{6p}{6x}) \times 2 \pi \times \frac{R^4}{4} = \frac{\pi}{8\mu} (-\frac{6p}{6x}) R^4$$

$$\therefore \text{ Average velocity, } \bar{u} = \frac{Q}{Area} = \frac{\frac{\pi}{8\mu}(-\frac{6p}{6x})R^4}{\pi R^2}$$
$$\bar{u} = \frac{1}{8\mu} \left(-\frac{6p}{6x}\right)R^2 \xrightarrow{(5)}$$

Dividing equation (4) by equation (5),

$$\frac{\text{Umax}}{\bar{u}} = \frac{-\frac{1}{4\mu} (\frac{6p}{6x})R^2}{\frac{1}{4\mu} (\frac{-5p}{6x})R^2} = 2.0$$

 \therefore Ratio of maximum velocity to average velocity = 2.0.

4. Drop of Pressure for a given Length (L) of a pipe

From equation (5), we have

$$\bar{u} = \frac{1}{8\mu} \left(-\frac{6p}{6x}\right) R^{2 \text{ or }} \left(-\frac{6p}{6x}\right) = \frac{8\mu\bar{u}}{R^{2}}$$

Integrating the above equation w.r.t. x, we get $\int_{1}^{1} \int_{1}^{1} \int_{1}^$

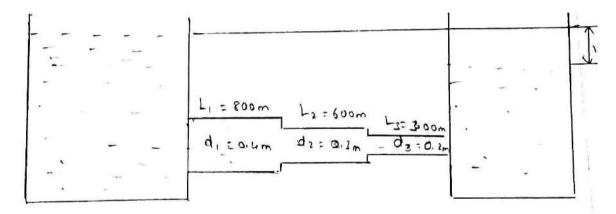
$$-\int_{2} dp = \int_{\frac{2}{R^{2}}} dx$$

- $[P_{1}-P_{2}] = \frac{1}{R^{2}} [X_{1}-X_{2}] \text{ or } (p_{1}-p_{2}) = \frac{8\mu\bar{u}}{R^{2}} [X_{1}-X_{2}]$

$$= \frac{8\mu\bar{u}}{R^{2}}L \qquad \{\therefore X_{2}-X_{1}=L \text{ from Fig.}\}$$
$$= \frac{8\mu\bar{u}L}{\left(\frac{D}{2}\right)^{2}}$$
$$(p_{1}-p_{2}) = \frac{32\mu\bar{u}L}{D^{2}}, \text{ where } p_{1}-p_{2} \text{ is the drop of pressure.}$$
$$\therefore \text{ Loss of pressure head} = \frac{p_{1}-p_{2}}{p_{g}}$$
$$\therefore \frac{p_{1}-p_{2}}{p_{g}} = h_{f} = \frac{\frac{g_{g}}{32\mu\bar{u}L}}{p_{g}D^{2}}$$

This Equation is called Hagen Poiseuille Formula.

8. Three pipes of 400 mm, 200 mm and 300 mm diameters have lengths of 400 m, 200 m, and 300 m respectively. They are connected in series to make a compound pipe. The ends of the compound pipe are connected with two tanks whose difference of water levels is 16 m. if the coefficient of friction for these pipes is same and equal to 0.005, determine the discharge through the compound pipe neglecting first the minor losses and then including them. (*Nov/Dec 2016*)



Solo:
Given: To tell head loss.
$$JI = 15 \text{ m}$$

=) $h_{1} + h_{0} + h_{0,2} + h_{0,1} + h_{1,1} + h_{1,2} = 15$
=) $\frac{0.5V_{1}^{2}}{29} + \frac{V_{1}^{2}}{29} + \frac{0.5V_{2}^{2}}{29} + \frac{0.5V_{2}^{2}}{29} + \frac{14fL_{1}V_{1}^{2}}{29d_{1}}$
 $+ \frac{14fL_{1}V_{2}^{2}}{29d_{2}} + \frac{14fL_{3}V_{3}^{2}}{29d_{3}} = 15 - - 0$
By continuity eqn:
 $Q = A_{1}V_{1} = A_{2}V_{2} = A_{3}V_{3}$
 $A_{1}V_{1} = B_{2}V_{2}$
 $T \times 0.2^{2}V_{3} = T \times 0.3^{2}V_{2}$
 $V_{1} = 0.562V_{2}$
Sub: V_{1} and V_{3} in D
=) $0.5(0.562V_{2})^{2} + \frac{6.25V_{3}^{2}}{29} + \frac{0.5V_{2}^{2}}{29} + \frac{0.5(2.25V_{3}^{2})}{29}$
 $+ \frac{14\times0.005\times000\times(0.562V_{3})^{2}}{29} + \frac{15\times0.05\times000\times0}{29\times05}$

$$= \frac{12.63V_{1}^{2}}{29} + \frac{5.0635}{29}V_{1}^{2} + \frac{10.5V_{1}^{2}}{29} + \frac{2.53V_{1}^{2}}{29}$$

$$+ \frac{12.63V_{1}^{2}}{29} + \frac{10V_{1}^{2}}{29} + \frac{151.575V_{1}^{2}}{29} = 15$$

=)
$$\frac{212.75 \text{ N}_2^2}{\text{ag}} = 15$$

=) $\text{N}_2^2 = \frac{15 \times 9.81 \times 2}{212.75}$
[$\text{N}_2 = 1.176 \text{ m/s}$

Discharge, $Q = A_{L} \times V_{2}$ = $\underline{\Pi} \times 0.3^{2} \times 1.17$

$$Q = 0.083 \text{ m}^3/\text{sec}$$

W.14.T,

$$\frac{L}{d^{5}} = \frac{L_{1}}{d_{1}^{5}} + \frac{L_{2}}{d_{2}^{5}} + \frac{L_{3}}{d_{3}^{5}}$$

$$\frac{1700}{d^{5}} = \frac{800}{(0.4)^{5}} + \frac{600}{(0.3)^{5}} + \frac{300}{(0.2)^{5}}$$

$$\frac{1700}{d^{5}} = 78125 + 246913.5 + 937500$$

$$\frac{1700}{d^{5}} = 1262538.5$$

$$d^{s} = 1.3468 \times 10^{-3}$$

$$d = 0.2665 m$$

$$= 0.2665 \times 1000 mm$$

$$d = 266.5 mm$$

9. A fluid of Visco sity 8 poise and specific gravity 1.2
is flowing through a circular pipe of diameter 100 mm.
The reasimum shear stress at 102 pipe wall is 210N/m².
Find:
(i) The pressure gradient.
(ii) Reynold's number of flow.
Solution:
Niscosity of fluid,
$$\mu = 8$$
 poise = 0.8 Ns/m².
Specific gravity = 1.2
 \therefore Mass density $e = 1.2 \times 1000 = 1200 \text{ kg/m^3}.$
Diameter of 152 pipe, $D = 100 \text{ mm} = 0.1 \text{ m}.$
Maxémum shear stress, $T_0 = 2100 \text{ kg/m^3}$
(j) The pressure gradient, $\frac{2P}{2Z}$:
We know that, $T_0 = -\frac{2P}{2X} \cdot \frac{(0.1/2)}{2}$
 $\Rightarrow \frac{2P}{2X} = -\frac{8400 \text{ N/m^2}}{2} \text{ per m}.$

(ii) The ownerage velocity,
$$\overline{u}$$
:
We know that, $\overline{u} = \frac{1}{2} \bigcup_{n \to \infty} \bigcup_{n \to \infty} \mathbb{R}^2$

$$= \frac{1}{2} \left[-\frac{1}{4\mu} \cdot \frac{\partial p}{\partial x} \cdot \mathbb{R}^2 \right]$$

$$= \frac{1}{2} \left[-\frac{1}{4\mu} \cdot \frac{\partial p}{\partial x} \cdot \mathbb{R}^2 \right]$$

$$= \frac{1}{2} \left[-\frac{1}{4\pi} \times (-8400) \times \frac{1}{4\pi} \times (-8400) \times \frac{1}{$$

1. The velocity distribution in the boundary layer is given by, $\frac{u}{U} = 2 \left(\frac{y}{\delta}\right) - \left(\frac{y}{\delta}\right)^2, \ \delta \ being boundary$ $<math display="block">\frac{u}{U} = 2 \left(\frac{y}{\delta}\right) - \left(\frac{y}{\delta}\right)^2, \ \delta \ being boundary$ Nov/Dec 2016

$$\delta^* = \delta/3$$

UNIT –III

DIMENSIONAL ANALYSIS AND MODEL STUDIES

1. Define dimensional homogeneity. (Nov/Dec 15,Non/Dec 11)

The dimensions of each term in an equation on both sides are equal. Thus if the dimensions of each term on both sides of an equation are the same the equation is known as dimensionally homogeneous equation

2. Derive the expression for Reynold's number? (Nov/Dec 15,12)

It is the ratio between inertia forces to the viscous force

 $Re=\rho vD/\mu$

3. Define Mach number?

It is defined as the square root of the ratio of the inertia force of a flowing fluid to the elastic force

4. State the Buckingham's π theorem? (Nov/Dec 12)

If there are n variables (dependent and independent) in a physical phenomenon and if these variables contain m fundamental dimensions, then these variables are arranged into (n-m) dimensionless terms called Pi terms

5. Name the methods for determination of dimensionless groups.

(Nov/Dec 11)

- i) Buckinghams pi theorem
- ii) Raleyritz method

6. State Froude's dimensionless number.(May/June 14)

It is defined as the square root of the ratio of inertia force of a flowing fluid to the gravity force

$$F_e = \sqrt{F_i/F_g}$$
.

7. Define dynamic similarity.

Dynamic similarity is said to exist between the model and the prototype if the ratios of corresponding forces at the corresponding points in the model are the same.

(Nov/Dec 14)

8. What are the advantages of model and dimensional analysis?

(May/June 09)

- 1. The performance of the structure or the machine can be easily predicted.
- 2. With the dimensional analysis the relationship between the variables influencing a flow in terms of dimensionless parameter can be obtained.
- Alternative design can be predicted and modification can be done on the model itself and therefore, economical and safe design may be adopted.

9. List the basic dimensional units in dimensional analysis.

(Nov/Dec 10)

- 1. Length(L)-meter
- 2. Mass(M)- kilogram
- 3. Time (T)- seconds

10. What are distorted models? State its merits and demerits.

(May/June 14)

A model is said to be distorted if it is not geometrically similar to its prototype. For a distorted model different scale ratios for the linear dimensions are adopted.

Merits

- 1. The vertical dimensions of the model can be measured accurately
- 2. The cost of the model can be reduced
- 3. Turbulent flow in the model can be maintained.

Demerits

1. The results of the distorted model cannot be directly transferred to its prototype.

11. Derive the scale ratio for velocity and pressure intensity using Froude model law. (Nov/Dec 2016)

$$(F_{e})_{rr} = (F_{e})_{p} \Rightarrow \underbrace{\sqrt{m}}_{\sqrt{g_{rr}L_{m}}} = \sqrt{g_{p}L_{p}}$$
Scale ratios based on Fronde number
(a) Scale ratio for time, $T_{rr} = \frac{T_{P}}{T_{m}} = \sqrt{L_{r}}$
(b) Scale ratio for acceleration,
$$a_{r} = \frac{V_{P}}{V_{ro}} \times \frac{T_{m}}{T_{p}} = \sqrt{L_{r}} \times \frac{1}{\sqrt{L_{r}}}$$

$$a_{r} = 1$$

scale ratio for pressure intensity,

$$P = \frac{Fonce}{Area} = \frac{PL^2 V^2}{L^2}$$

$$P = PV^2$$

$$Pr = \frac{Pp}{Pm} \cdot \frac{Vp^2}{Vm^2}$$
for same fluid, $Pp = Pm$

$$Pr = \frac{Vp^2}{Vm^2} = \sqrt{Lr^2} = Lr$$

$$Pr = Lr$$

1. Using Buckingham's TI_{-} theorem, show that the velocity through a circular orifice is given by $V = \sqrt{2gH} \ \mathcal{P}[D/H', \frac{M}{PVH}]$, where H is the head causing flow, D is the diameter of the orifice, M is co-efficient of Viscosity, P is the mass density and g is the acceleration due to gravity. (16) [Apr/May - 2010].

> Given: V & a function of H, D, M, P and g $V = f(H, D, M, P, g) (OH) \rightarrow (i)$ $f_1 \in V, H, D, M, P, g) \longrightarrow (ii)$ Total ho. of Vaeiable; N = 6. dimensions of each Vaeiable; $V = LT^{-1}$; $M = ML^{-1}T^{-1}$ H = L; $P = ML^{-3}$ D = L; $g = LT^{-2}$ No. of fundamental dimensions M = 3 \therefore Number of T-terms = h-m= 6-3 = 3

Equation (i) can be written as $f_{1}(T_{1}, T_{2}, T_{3}) = 0$. Each T_{1} -term. Contains m+1 Variables, where m=3and is also equal to repeating Variables, Here V is a dependent Variable and herce should not be detected as supeating Variable. Choosing $H_{1}g_{1}p$ as suppeating Variable, We get three T_{1} -terms as,

$$T_{I} = H^{a_{I}}, g^{b_{I}}, \rho^{c_{I}}, \vee . \longrightarrow @$$

$$T_{Q} = H^{a_{2}}, g^{b_{2}}, \rho^{c_{2}}, D \longrightarrow @$$

$$T_{g} = H^{a_{3}}, g^{b_{3}}, \rho^{c_{3}}, M \longrightarrow @$$

First II. term :

$$\widehat{U}_{\overline{1}} = H^{\alpha_1}, g^{\beta_1}, p^{\alpha_1}, V.$$

Substituting dimensions on both sides,

$$M^{\circ} L^{\circ} T^{\circ} = L^{\alpha_{1}} (LT^{-2})^{b_{1}} (ML^{-3})^{c_{1}} LT^{-1}$$

Equating the power of H, L, T on both rides,

Power of M,
$$0 = C$$
.
Power of L, $0 = a_1 + b_1 - 3c_1 + 1$
 $a_1 = -b_1 + 3c_1 - 1$
 $= 1/2 + 0 - 1$; $a_1 = -1/2$

Power of T, $O = -2b_1 - 1$ $b_1 = -\frac{1}{2}$

Third Π_{-} term : $\Pi_{3} = H^{a_{3}} \cdot g^{b_{3}} \cdot \rho^{c_{3}} \cdot M \cdot M^{o}L^{o}T^{o} = L^{a_{3}} \cdot (LT^{-2})^{b_{3}} \cdot (ML^{-3})^{c_{3}} \cdot ML^{-1}T^{-1}$

Fqu. the power of M.L.T on both,
Power of M = 0 =
$$(g + 1)$$
; $[\underline{G_{3} = -1}]$
Power of L = 0 = $93 + \frac{1}{9} - \frac{9}{9} - \frac{1}{9} - \frac{3}{9} - \frac{1}{9}$
Power of T = $0 = -\frac{2}{9} - \frac{1}{9} - \frac{1}{9}$; $[\underline{b_{3} = -\frac{1}{2}}]$
Gub. the Abc Values on The term,
 $\overline{T_{3}} = \frac{M}{H^{3/2}}, \ g^{-\frac{1}{2}}, \ p^{-1}, M$
 $\boxed{\overline{T_{3}} = \frac{M}{H^{3/2}}, \ p^{-\frac{1}{2}}, M}$ (On) $\frac{M}{HP \sqrt{gH}} = \frac{MV}{HP \sqrt{gH}}$
 $\boxed{\overline{T_{3}} = \frac{M}{H^{3/2}}, \ p^{-\frac{1}{2}}, M}$
 $[\overline{T_{3}} = \frac{M}{H^{9/2}}, \overline{T_{1}}]$ (On) $\frac{M}{HP \sqrt{gH}} = \frac{MV}{HP \sqrt{gH}}$
 $\boxed{T_{3}} = \frac{M}{H^{9/2}}, \ \overline{T_{1}}, \ \overline{T_{1}}, \ \overline{T_{1}}, \ \overline{T_{2}}, \ \overline{T_{3}} = \frac{M}{H^{9/2}}, \ \overline{T_{1}}]$
Gub.Hituiting the Values of $\overline{T_{1}}, \overline{T_{3}}, \ \overline{T_{3}}, \ \overline{T_{3}}, \ \overline{T_{3}}, \ \overline{T_{3}} = 0$ (OR)
 $f_{1}(\frac{V}{4\overline{gH}}, \frac{D}{H}, \ \overline{T_{1}}, \frac{M}{HPV}) = 0$ (OR)
 $\sqrt{\overline{gH}} = \Phi \left[\frac{D}{H}, \ \overline{T_{1}}, \ \frac{M}{HPV}\right]$ (OS)
 $V = \sqrt{2gH} \quad \Phi \left[\frac{D}{H}, \ \overline{T_{1}}, \ \frac{M}{HPV}\right]$
Hultiplying by a Constant does not change the
Character of $\overline{T_{1}}$ terms.
The Power developed by hydraulic machine in
found to depend on the head H, gliow sate Θ ,
dervity P , Aped N, summer diameter D and acceleration
due to gravity g . Obtain suitable dimensionlers
Parameters to constant experimental premets. \mathbb{C} [6]
 $(NOV/DEC-2014]$
Solution:
 $P = f(H, \Theta, P, N, D, g) \longrightarrow O$

Contract of

 $f_{1} (\mathcal{P}, H, Q, P, N, \mathcal{D}, g) = 0 \longrightarrow @$

2.

Tobal. no.9 Variables
$$n: 4$$
.
No.9 Jundamental dimensions $m = 3$
 \therefore No.9 Ti - terms $= h - m$
 $= 7 - 3 \Rightarrow 4$.
 $f_1 (T_1, T_2, T_3, T_4) = 0 \longrightarrow (lil)$
 $T_1 = H^{a_1} N^{b_1} p^{c_1} P \longrightarrow 0$
 $T_2 = H^{a_2} N^{b_3} p^{c_3} Q \longrightarrow 0$
 $T_3 = H^{a_3} N^{b_3} p^{c_4} Q \longrightarrow 0$
 $T_4 = H^{a_4} N^{b_4} p^{c_4} D \longrightarrow 0$
 $T_5 = H^{a_5} N^{b_7} p^{c_4} D \longrightarrow 0$
dimensions of each Variables.
 $H = L; N = T^{-1}; P = HL^{-3}$
 $P = ML^2 T^{-3}, Q = L^3 T^{-1}, g = LT^{-2}, D = L$.
First T. term:
 $T_1 = H^{a_1} N^{b_1} p^{c_1} P \longrightarrow 0$
applying dimensions on both sides
 $M^{b_1} P^{c_1} T^{-1} (T^{-1})^{b_1} (ML^{-3})^{c_1} ML^2 T^{-3}$.
Equating Power of M.L.T on both.
Power of $H = 0 = c_1 + 1 \ddagger (c_1 = -1)$
Power of $L = 0 = a_1 - 3c_1 + 2$
 $a_1 = 3c_1 - 2$
 $\frac{z - 3 - 2}{a_1 = -5}$

Power of
$$T = 0 = -b_1 - 3$$

 $\begin{bmatrix} b_1 = -3 \end{bmatrix}$
Substituting as $b_1 c_1$ value in equation (1).
 $T_1 = H^{-5} \cdot N^{-3} \cdot P^{-1} \cdot P$
 $T_1 = \frac{P}{H^5 N^3}$
Second T_1 -term:
 $T_2 = H^{a_2} \cdot N^{b_2} \cdot P^{c_2} \cdot Q \longrightarrow (2)$
applying dimension on both soldes,
 $H^0 L^0 T^0 = (L)^{a_2} \cdot (T^{-1})^{b_3} \cdot (HL^{-3})^{c_2} \cdot L^3 T^{-1}$.
Equating Power of $H_1 + L_1 T$ on both soldes.
Power of $H = \begin{bmatrix} c_2 = 0 \end{bmatrix}$
Power of $L = a_2 - 3c_2 + 3 = 0$
 $a_2 = 3c_2 - 3$
 $\begin{bmatrix} a_2 = -3 \end{bmatrix}$
Power of $T = -b_2 - 1$
 $\begin{bmatrix} b_2 = -1 \end{bmatrix}$
Substituting a_2, b_3, c_3 value in equation (2)
 $T_2 = (H)^3 \cdot N^3 \cdot P^3 \cdot 3$
Third T_1 form:

 $\begin{aligned} \overline{\Pi_{3}} &= (H)^{a_{3}} \cdot (N)^{b_{3}} \rho^{c_{3}} \cdot \theta \longrightarrow 3 \\ \text{applying dimension on both fides,} \\ M^{o}L^{o}T^{o} &= (L)^{a_{3}} \cdot (T^{-1})^{b_{3}} \cdot (HL^{-3})^{c_{3}} \cdot LT^{-2} \end{aligned}$

Power of
$$M = \begin{bmatrix} c_3 & c_3 \\ a_3 & c_3 & c_3 + 1 \\ a_3 & c_3 & c_3 - 1 \end{bmatrix}; \begin{bmatrix} a_3 & c_3 & -1 \\ a_3 & c_3 & c_3 & c_3 \end{bmatrix};$$

Power of $T = -b_3 - 2 ; \begin{bmatrix} b_3 & c_3 & c_3 \\ b_3 & c_3 & c_3 \end{bmatrix};$
Substituting as, bs, cs Value in equ (3)
 $TI_3 = H^{-1}, N^{-2}, P^0, 9$.
 $TI_3 = \frac{9}{N^2 H}$
Fourth To term :

Fourth 1 $T_{4} = (H)^{a_{4}} (N)^{b_{4}} (P)^{c_{4}} D \longrightarrow \emptyset$ applying dimension on both sides, $M^{0}L^{0}T^{0} = (L)^{94} \cdot (T^{-1})^{64} \cdot (HL^{-3})^{C_{4}} \cdot L$ equating the power of M. L.T on both. Power of $M = \begin{bmatrix} C_{4} = 0 \end{bmatrix}$ power of L = a4 - 8 c4 + 1 a4 = 0-1 [a4 = -1] , power of T = - by = 0. ; [64 = 0] Substituting at, 64. C4 values on equ (4) TI4 = H-1, Nº. Pº. D [E14 = D/H Substitute To Values in equation. (iù) f (ຎ, . ຎ₂, ຎ₃, ຎµ) ≃ 0.

$$f\left[\frac{P}{H^{S},N^{3},P},\frac{Q}{H^{3},N},\frac{9}{N^{2}H},\frac{D}{H}\right] = 0$$

$$\frac{P}{H^{S},N^{3},P} = P\left[\frac{Q}{H^{3},N},\frac{9}{N^{2},H},\frac{D}{H}\right]$$

$$P = H^{5}N^{3}P P\left[\frac{Q}{H^{3},N},\frac{Q}{N^{2},H},\frac{9}{H}\right]$$

3. Derive on the basis of dimensional analytis suitable parameters to present the thrust developed by a propeller. Assume that the thrust P depends on the angular velocity us, Speed of advance V, diameters D, dynamic Viscosity M, mass density P, and elasticity of the fluid medium which can be denoted by the speed of sound in the medium 'c'. [16] [Nov/Dec - 2012]

folution:

Thrust P ù a function of w, V, D, M, P, C. P = $f(w, V, D, M, P, C) \longrightarrow (i)$ $f_1 (P, w, V, D, M, P, C) = 0 \longrightarrow (ii)$ \therefore Total no.of Variables n = 4. dimensions of each Variable, $P = HLT^{-2}$; $w = T^{-1}$; $V = LT^{-1}$; D = L. $M = HL^{-1}T^{-1}$; $P = ML^{-3}$; $C = LT^{-1}$ \therefore No.of fundamental dimensions, m = 3. Total. No.of TL terms = $n-m \Rightarrow 4-3$ $\Rightarrow 4$

Hence equation () can be written as,

$$f_1 (T_1, T_2, T_3, T_4) = 0 \rightarrow (10)$$

 $T_1 = D^{\alpha_1}, v^{\beta_1}, p^{\beta_1}, p$
 $T_2 = D^{\alpha_2}, v^{\beta_2}, p^{\beta_3}, w$
 $T_3 = D^{\alpha_3}, v^{\beta_3}, p^{\beta_3}, M$
 $T_3 = D^{\alpha_4}, v^{\beta_4}, p^{\beta_4}, q$
 $T_4 = D^{\alpha_4}, v^{\beta_4}, p^{\beta_4}, q \rightarrow 0$
applying dimensions on both sides,
Fower of $M = 0 = c_1 + 1$; $(c_1 = -1)$
Power of $L = 0 = a_1 + b_1 - 3c_1 + 1$
 $a_1 = -b_1 + 3c_1 - 1$
 $= 2 - 3 - 1 = -2$. $a_1 = -2$
Substituting the values of a_1, b_1 is c_1 in quill
 $T_1 = D^{-2}, V^{-2}, p^{-1}, p$
 $T_1 = D^{\alpha_2}, V^{-2}, p^{-1}, p$
Second T_1 -term : $T_2 = D^{\alpha_2}, v^{\beta_2}, p^{\beta_2}, w$
 $applying dimension on both sides,
 $H^0L^0, T^0 = L^{\alpha_2}, (LT^{-1})^{\beta_2}, (HL^{-3})^{\beta_2}, T^{-1}$$

Equating the power of MiL, Tonboth,
Power of M = 0 =
$$c_R$$
; $c_2=0$
Power of L = 0 = $a_R + b_2 - 3c_2$
 $a_2 = -b_2 + 3c_2$.
 $= 1 + 0 = 1$
 $a_2 = 1$

Power of
$$T = 0 = -b_2 - 1$$

 $\boxed{b_2 = -1}$
Substituting the value of a_2 , b_2 , e_2 in \overline{h}_2 .
 $\overline{h}_2 = D^1$. Y^{-1} . p^0 . We
 $\boxed{T_2 = \frac{DW}{V}}$
Third TI -term;

Third II - term:

$$TI_{3} = D^{a_{3}} \cdot v^{b_{3}} \cdot \rho^{c_{3}} \cdot M \cdot \longrightarrow \textcircled{3}$$
applying dimension on both,

$$N^{0}L^{0}T^{0} = L^{a_{3}} \cdot (LT^{-1})^{b_{3}} \cdot (ML^{-3})^{c_{3}} \cdot ML^{-1}T^{-1}$$
Equating the power of $M, L, \& T$ on both,
Power of $M = 0 = c_{3} + 1 ; [c_{3} = -1]$
Power of $L = 0 = a_{3} + b_{3} - 3c_{3} - 1$

$$a_{3} = -b_{3} + 3c_{3} + 1$$

$$= 1 - 3 + 1 = -1$$
Power of $T = 0 = -b_{3} - 1$

$$[b_{3} = -1]$$
Power of $T = 0 = -b_{3} - 1$

Substituting the Values of
$$a_3$$
, $b_3 \approx c_3$ in ll_3
 $Tl_3 = D^{-1} \cdot V^{-1} \cdot P^{-1} \cdot u$

$$\overline{II_3} = \frac{M}{DVP}$$

Fourth IT. term : $T_{A} = D^{a_{4}} \cdot v^{b_{4}} \rho^{c_{4}}, c.$ applying dimensions on both sides, MOLOTO = L aq. (LT-1) b4. (ML-3), LT Equating the power of M, L, Tonboth, sides. Power of M = 0 = C4 ; [C4=0] Power of L = 0 = a4 + 64 - 3c4 + 1 a4 = -64 + 3c4 -1 = 1+0-1 =0 a4 = 0 Power of T = 0 = -64-1 64 = -1 Substituting the values of a4, 64, C4 in equ (A) WH = DO, VH. PO, C = C/V $\overline{u}_{4} = C/V$ Substituting the values of Tri Dai To & Dy inequ (i) $f_{i}\left(\frac{p}{D^{2}v^{2}\rho}, \frac{Du^{2}}{v}, \frac{M}{v}, \frac{e}{v}\right) = 0 \quad (0\pi)$ $\frac{P}{D^{2}V^{2}P} = P\left[\frac{DW^{2}}{V}, \frac{M}{DVP}, \frac{c}{V}\right] (09)$ P = D^QV^Q P Q [DW, M, C]

Gliven:
Dia of Prototype (Dp) = 1.5m.
Vircority of prototype
$$j = 3 \times 10^{-2} poirce$$

(Np) j
 $R_p = 3000 L/s$; $3 m^3/s$
 $Sp = 0.9$
... Density of Prototype (Pp) = $Sp \times 1000$
 $= 0.9 \times 1000$
 $= 0.9 \times 1000$
 $= 0.9 \times 1000$
 $= 0.9 \times 1000$

Find :

4.

Velocity so state of glow in model. Non = ? Ron = ?

Formula required !

$$\frac{P_{m} V_{m} D_{m}}{M_{m}} = \frac{P_{p} V_{p} D_{p}}{M_{p}}$$

$$\frac{Q_{m} = A_{m} \times V_{m}}{Q_{m}}$$

Solution :

For pipe flow, the dynamic similarity will be obtained if the Reynold's Number in the model of prototype are equal.

Flence Using equation.,

$$\frac{P_{m} V_{m} D_{m}}{M_{m}} = \frac{P_{p} V_{p} D_{p}}{M_{p}}$$

$$\frac{V_{m}}{V_{p}} = \frac{P_{p}}{P_{m}} \cdot \frac{D_{p}}{D_{m}} \cdot \frac{M_{m}}{M_{p}} \qquad \begin{array}{l} I \quad \text{for plpe}}{Linear Dimension intervention} \\ = \frac{900}{1000} \times \frac{1.5}{0.15} \times \frac{1 \times 10^{-2}}{3 \times 10^{-2}} \\ = \frac{900}{1000} \times 10 \times \frac{1}{3} = 3.0 \\ V_{p} = \frac{Rate}{Q} q \cdot \frac{1}{9} \log \ln P xototype \left(Q_{p}\right)}{Area q} = \frac{3}{T/4} \left(D_{p}\right)^{2} \\ V_{p} = \frac{3}{T/4} \left(1.5\right)^{2} \Rightarrow \frac{3 \times H}{T \times d.R5} = 1.697 \text{ m/s} \\ V_{m} = 3 \times V_{p} \Rightarrow 3 \times 1.697 = 5.091 \text{ m/s} \\ Rate q \cdot \frac{1}{9} \log theough 2 \cdot \frac{1}{9} \left(Q_{m}\right) = \frac{A_{m} \times V_{m}}{M_{p}} \\ = \frac{T}{4} \left(0.15\right)^{2} \times 5.091 \\ = 0.0899 \text{ m}^{3}/s \\ = 0.0899 \text{ x} 1000 \text{ lit/s} \\ = 89.9 \text{ lit/s}. \end{array}$$

Result :

5. The Efficiency 7 of a fan depends on the dentity
P, the dynamic Viscosity 11 of the fluid. the angular
Velocity we, diameter D of the Scotor. and the discharge
Q. Appens 7 interms of dimensionless parameters.
Use Rayleights method. (16)
Solution':

$$J = K \cdot P^{q} \cdot u^{b} \cdot u^{c} \cdot D^{d} \cdot Q^{c} \rightarrow 0$$

Where $K = Non$ dimensional constant.
dimensions of each Variables.
 $P = ML^{-3}$; $M = ML^{-1}T^{-1}$; $W = T^{-1}$;
 $D = L$; $Q = L^{3}T^{-1}$

Substituting the dimensions on both sides. in equ $(D = K (ML^{-3})^{a}, (ML^{-1}T^{-1})^{b}, (T^{-1})^{c}, (L)^{d}, (L^{3}T^{-1})^{b}$

Power of H,
$$0 = a+b$$

Power of L, $0 = -3a - b + d + 3e$
Power of T, $0 = -b - c - e$
Hence expressing a.e., & d in terms of b & e,
we get,
 $a = -b$
 $b = -(b+e)$
 $d = 8a + b - 3e$
 $= -3b + b - 3e$
 $= -2b - 3e$.
Substituting a.b.d values in equation ()

We get:

$$\eta = k. p^{-b}, u^{b}, u^{-(b+e)}, D^{-2b-3e}, e^{e}$$

 $= k. p^{-b}, u^{b}, u^{-b}, u^{-e}, D^{-2b}, D^{-3e}, e^{e}$
Remut:
 $= k\left(\frac{u}{pusp^{2}}\right), \left(\frac{Q}{usp^{3}}\right)^{e} = \varphi\left[\left(\frac{u}{pusp^{2}}\right), \left(\frac{Q}{usp^{3}}\right)\right]$
6. Using Buckinghami π theorem, show that the velocity
through a circular oxidice is given by $V = VagH \Rightarrow \left[\frac{D}{H}, \frac{M}{eVH}\right]$,
where H is the head causing flow, D is the diametric
of the existic, μ is the co-efficient of Visconstry, e is the
mass density and g is the acceleration due to gravity.
3chibion: Given: V is a function of H, D, A, P, g April/May 2017
 $V = f(H, D, H, P, g) = 0$ (1)
c) Total number of π -terms = p_{-} m = $(-3=3)$.
Equation (1) can be conflice as,
 $f_{1}(\pi_{1}, \pi_{2}, \pi_{3}) = 0$. (2)
Each π term bas M^{-2} superting Variables and
 $m_{H} = 3H = H$ total Variables are H, g, P .
 $\pi_{H} = H^{a_{1}} g^{b_{1}} e^{C_{1}} V$
 $\pi_{H} = H^{a_{2}} g^{b_{2}} e^{C_{2}} D$

$$\overline{\Lambda_3} = H^{\alpha_1} g^{\beta_2} e^{\zeta_1} H$$

Analysis $g = \overline{\lambda} + \frac{1}{12\pi\pi_{23}}$:
First $\overline{\lambda} + \frac{1}{12\pi\pi_{23}}$: $\overline{\Lambda_1} = H^{\alpha_1} g^{\beta_2} e^{\zeta_1} V$
substituting dimensions on both sides,
 $M^{\alpha}L^{\alpha}T^{\alpha} = L^{\alpha_1} (LT^{-2})^{\beta_1} (ML^{-3})^{\alpha_1} (LT^{-1})$
Equables powers $g = M, L, T$ on both sides
Power $g = M, D = C \quad C = 0$
Power $g = L, D = a, tb_1 - 3c_1 + 1; D = a, tb_1 + 1, 0 = a_1 - V_2$
Rower $g = T, 0 = -2b_1 - 1, 2b_1 = -1; b_1 = -V_2, a_1 = -V_2$
substituting the value $c_1 = a, b_1, c_1$ in $\overline{\Lambda_1}$
 $\overline{\Lambda_1} = t^{-V_2} g^{-V_2} e^{\alpha_1} V$
 $\overline{\Lambda_1} = \frac{V}{\sqrt{gH}}$
Second $\overline{\lambda}$ terms:
Nubstituting dimensions on both sides
Power $g = M, 0 = C_1 \Rightarrow C_1^{-2}$
Reading powers of M, L, T on both sides
Power $g = M, c_1 = C_1 \Rightarrow C_1^{-2}$
Reader $af = M, c_1 = 0 = a_1 + 1 \Rightarrow a_1 = -1$
Power $g = L, 0 = a_1 + b_1 - 3c_1 + 1 \Rightarrow 0 = a_1 + 1 \Rightarrow a_1 = -1$
Power $g = L, 0 = a_1 + b_1 - 3c_1 + 1 \Rightarrow 0 = a_1 + 1 \Rightarrow a_1 = -1$
Power $g = L, 0 = -2b_1 \Rightarrow b_1 = 0$
Substituting a_1, b_1, c_1 in $\overline{\Lambda_2}$
 $\overline{\Lambda_2} = \frac{D}{H}$
Third $\overline{\Lambda}$ terms:
substituting H_2 dimensions on both sides.
 $M^{\alpha}L^{\alpha}T^{\alpha} = L^{\alpha_3} (LT^{-2})^{\beta_3} (ML^{-3})^{\alpha_3} ML^{\alpha_1}T^{-1}$
Equaling powers of M, L, T on both side.
Power $g = M, 0 = c_2 + 1 \Rightarrow c_{3} - J_2$
Power $g = M, 0 = c_2 + 1 \Rightarrow c_{3} - J_2$
Power $g = L, 0 = a_1 + b_2 - 3c_3 - J_2 + 2 + a_{32} - 3J_3$
Power $g = L, 0 = a_1 + b_2 - 3c_3 - J_2 + 2 + a_{32} - 3J_3$

j.

ł

7.

No. of Variables, n= 7
No. of fundamental dimensions, m= 3
No. of
$$\pi$$
-terms = n-m = 7.3
Eqp. (1) can be writted as. $f_1(\pi_1, \pi_2, \pi_3, \pi_4) = 0;$
 $\pi_{-\text{terms}}: \pi_1 = D^{-1} \vee^{b_1} e^{c_1} \Delta p$
 $\pi_{2} = D^{a_2} \vee^{b_2} e^{02} \lambda$
 $\pi_3 = D^{a_4} \vee^{b_2} e^{02} \lambda$
 $\pi_4 = D^{a_4} \vee^{b_4} e^{a_4} k$
Results: $\pi_1 = \frac{\Delta p}{Rv^2} = \pi_3 = \frac{\mu}{Dv_R}$
 $\pi_{2} = \frac{\lambda}{D} = \pi_{4} = \frac{k}{D}$
 $\frac{\Delta p}{Rv^2} = \phi \left[\frac{\lambda}{D}, \frac{\mu}{Pv_R}, \frac{k}{D}\right]$

PART-C

1. The aerodynamic drag of a new sports car is to be predicted at a speed of 50.0 mi/h at an air temperature of 25° C. Automotive engineers build a one- fifth scale model of the car to test in a wind tunnel. It is winter and the wind tunnel is located in an unheated building; the temperature of the wind tunnel air is only about 5°C. Determine how fast the engineers should run the wind tunnel in order to achieve similarity between the model and the prototype.

SOLUTION

We are to utilize the concept of similarity to determine the speed of the wind tunnel. Assumptions 1. Compressibility of the air is negligible (the validity of this approximation is discussed later). 2. The wind tunnel walls are far enough away so as to not interfere with the aerodynamic drag on the model car. 3. The model is geometrically similar to the prototype. 4. The wind tunnel has a moving belt to simulate the ground under the car, as in Fig. (The moving belt is necessary in order to achieve kinematic similarity everywhere in the flow, in particular underneath the car.)

Properties

For air at atmospheric pressure and at T = 25°C, $\rho = 1.184 \text{ kg/m}^3$ and $\mu = 1.849 \text{ x} 10^{-5} \text{ kg/m.s.}$ Similarly, at T = 5°C, $\rho = 1.269 \text{ kg/m}^3$ and $\mu = 1.754 \text{ x} 10^{-5} \text{ kg/m} \cdot \text{s.}$ Since there is only one independent π in this problem, the similarity equation holds if $\pi_{2\text{m}} = \pi_{2\rho}$

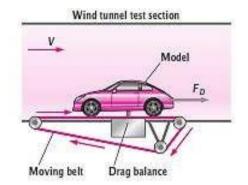
$$\Pi_{\mathbf{2},m} = \mathbf{R}\mathbf{e}_m = \frac{\rho_m V_m L_m}{\mu_m} = \Pi_{\mathbf{2},p} = \mathbf{R}\mathbf{e}_p = \frac{\rho_p V_p L_p}{\mu_p}$$

which can be solved for the unknown wind tunnel speed for the model tests, Vm,

 $Vm = Vp \ (\mu_m/\mu_p)(\rho_p/\rho_m)(L_p/L_m)$

Substituting the values we have,

$V_m = 221 \text{ m/h}$



Thus, to ensure similarity, the wind tunnel should be run at 221 mi/h (to three significant digits). Note that we were never given the actual length of either car, but the ratio of Lp to Lm is known because the prototype is five times larger than the scale model. When the dimensional parameters are rearranged as non-dimensional ratios (as done here), the unit system is irrelevant. Since the units in each numerator cancel those in each denominator, no unit conversions are necessary.

UNIT –V

PUMPS

1. What is meant by Cavitations?

It is defined phenomenon of formation of vapor bubbles of a flowing liquid in a region where the pressure of the liquid falls below its vapor pressure and the sudden collapsing of theses vapor bubbles in a region of high pressure.

2. Define Slip of reciprocating pump. When the negative slip does occur?

(Nov/Dec 15,12,May/June 14)

The difference between the theoretical discharge and actual discharge is called slip of the pump.

But in sometimes actual discharge may be higher then theoretical discharge, in such a case coefficient of discharge is greater then unity and the slip will be negative called as negative slip.

3. What is meant by NSPH?

(Nov/Dec 14,May/june 14)

(May/june 09)

(May/june 11)

(April/may 08)

Is defined as the absolute pressure head at the inlet to the pump, minus the vapour pressure head plus velocity head

4. What is indicator diagram?

Indicator diagram is nothing but a graph plotted between the pressure head in the cylinder and the distance traveled by the piston from inner dead center for one complete revolution of the crank

5. What are rotary pumps?

Rotary pumps resemble like a centrifugal pumps in appearance. But the working method differs. Uniform discharge and positive displacement can be obtained by using these rotary pumps, It has the combined advantages of both centrifugal and reciprocating pumps.

6. What is meant by Priming?

The delivery value is closed and the suction pipe, casing and portion of the delivery pipe upto delivery value are completely filled with the liquid so that no air pocket is left. This is called as priming.

Nov/Dec 15

7. Define speed ratio, flow ratio

Speed ratio: It is the ratio of peripheral speed at outlet to the theoretical velocity of jet corresponding to manometric head.

Flow ratio: It is the ratio of the velocity of flow at exit to the theoretical velocity of jet corresponding to manometric head.

8. Mention the main parts of the centrifugal pump.

(Nov/Dec 12)

- 1. Impeller
- 2. Casing
- 3. Suction pipe with foot valve and a strainer
- 4. Delivery pipe

9. What is an air vessel? What are its uses?

May/june 12,Nov/Dec 10)

It is a closed chamber containing compressed air in the top portion and liquid at the bottom of the chamber

Uses

To obtain a continuous supply of liquid at a uniform rate

To save a considerable amount of work in overcoming the frictional resistance in the suction pipe

10. Specific speed of a centrifugal pump.(Nov/Dec 09)

It is defined as the speed of a geometrically similar pump which would deliver one cubic metre of liquid per second against a head of one metre.it is denoted by 'Ns'

PART-B

1. The cylinder base diameter of a single acting
secipeocating pump is 150mm and it's diacke is 300mm.
The pump Mans at 50 ppm and lifts water through
a height of 25m. The delivery pipe 22m long is 100 mm in
diameter. find the discharge and the thrasitical power
sequired to run the pump. 21 actual discharge 4.2 fls.
Find the penentage of stip. (16) [Nov! Dec - 2012]
Also delemine the acculation hand at the seguing smiddle of
Given: the delivery stake.
diameter (d) = 150 mm = 0.15m
length of delivery pipe (24) = 300mm = 0.3m
Macking
Speed (N) = 50 r.pm.
(Height (H) = 25m
length of delivery pipe (24) = 100 mm = 0.1m
Actual disclarge Rast = 4.2 fls = 0.0042 ml/s.
Find:
(i) Theosetical discharge (QHL)
(ii) percentage of slip ('4')
Folmula:
(i) Q_{HL} = AlN
(iii) Presentage of slip ('4')
Folmula:
(i) Q_{HL} = AlN
(ii) Theosetical discharge (QHL)
(ii) P = Pg Sh xH
1000
Solution:
(i) Theosetical discharge (QHL)

$$Q_{HL} = \frac{ALN}{60}$$

 $A = T/A (d^{1})$
 $= T/A (0.15)^{2}$
 $= 0.1464 m^{2}$.

Q_{th} = 0.1767 x 0.3x 80
$$\Rightarrow$$
 0.0044175 Å/s
60
Q_{th} = 4.417 L[s]
(i) Theoretical Prover (P) = P g G th xH (ost) (workdowe)
sec
1000 x 9.81 x 0.00441 x 25
Power (P) = 1.0833 Km
(ii) Percentage of slip (Y) = (G th G th k 100
 $= (4.4175 - 4.2) \times 100$
 $= (4.4175 - 4.2) \times 100$
 $= (4.4175 - 4.2) \times 100$
 $A.4175$ $\Rightarrow 4.92 Y.$
 $Y. Of slip = 4.92 Y.$
 $Y. Of slip = 4.92 Y.$
(iv) A culvation head at the beginning of delivery dreake
had = ld x A x w²r. Coso
 $ad = \frac{1}{60} \div \frac{28x 50}{60} \Rightarrow 5.286 T/s$
 $w^{2} = 5.286 Trad/s$

$$T = H_2 = \frac{0.3}{2} \Rightarrow 0.15 m$$

$$h_{ad} = \frac{22}{9.81} \times \frac{0.01767}{0.007854} \times 5.286^2 \times 0.15 \times Cos0$$

= 20,75x coso

dt the beginning og delevery dræcke
$$0=0^{\circ}$$
 is herre $(000)=1$
 $\boxed{had} = 20.75 \text{ m}$ $[f'(010)=1]$
(i) Acceleration head at the middle og delivery blocke
 $0=90^{\circ}$ and herre $(000)=0$
 \therefore had $= 20.75 \times 0$
 $\boxed{had} = 0$
Renelt: $Q_{1h} = 4.417 \text{ L/s}$ had at beginning $= 20.75 \text{ m}$
 $P : 1.00833 \text{ KW}$ had at beginning $= 20.75 \text{ m}$
 $P : 1.00833 \text{ KW}$ had at middle $= 0$
 1.00833 KW had at middle $= 0$
 1.0083 M had at middle $= 0$
 1.0083 M had 1.0083 M had 1.0083 M
 $1.009 \text{ The pump CN} = 507 \text{ P.m}$
Actual dicharge $(Q_0) = 0.01 \text{ mB/s}$
 $Dia. 09 \text{ Piston}$ $(D) = 200 \text{ mm} = 0.200 \text{ M}$
 $Area (A) = \frac{17}{4} (0.2)^2$
 $= 0.0314 \text{ m}^3$
 $L = 4000 \text{ mm} = 0.4000$
Find 1.003 KW at $= 4000 \text{ mm} = 0.4000$
 1.00314 m^3
 $L = 4000 \text{ mm} = 0.4000$

2.

Foenula:

$$Q_{1} = \frac{ALN}{60}$$

$$C_{d} = \frac{Q_{ad}}{Q_{1}}$$

$$S^{(1)} = Q_{1k} - Q_{act}$$
(1) Theoretical discharge $(Q_{1k}) = \frac{ALN}{60}$

$$= \frac{QR31416 \times 0.40 \times 50}{60}$$

$$= 0.01047 m^{3}/s.$$
(ii) Co efficient of discharge
$$Q_{1} = \frac{Q_{act}}{Q_{1k}} = \frac{0.01}{0.01047} = 0.955.$$
(iii) S^{(1)} = Q_{1k} - Q_{act}
$$= 0.01047 - 0.01$$

$$= 0.00047 m^{3}/s$$
Remutt :
(i) Theoretical Discharge $(Q_{1k}) = 0.01047 m^{3}/s$
(ii) (a efficient of discharge $(Q_{1k}) = 0.01047 m^{3}/s$

N = 1200 γpm. Θ = 20°; φ = 30°

Find :

Formula:

$$W = \frac{1}{9} V_{w_2} u_2$$

Solution:

.

$$V_{f_{1}} = V_{f_{2}}.$$

$$U_{1} = \frac{\Pi 2N}{60} = \frac{\Pi \times 0.20 \times 1200}{60}$$

$$U_{1} = 12.56 \text{ m/s}$$

$$U_{2} = \frac{\Pi D_{2}N}{60} = \frac{\Pi \times 0.40 \times 1200}{60}$$

$$U_{2} = 25.13 \text{ m/s}$$

$$\tan 0 = \frac{V_{f_{1}}}{U_{1}} = \frac{V_{f_{1}}}{12.56}$$

$$V_{f_{1}} = 12.56 \times \tan 20$$

$$= 4.577 \text{ m/s}$$

$$V_{f_{1}} = V_{f_{2}} = 4.574 \text{ m/s}$$

$$\tan \varphi = \frac{V_{f_{2}}}{U_{2} - V_{w_{2}}} = \frac{4.574}{25.13 - V_{w_{2}}}$$

$$25.13 - V_{w_{2}} = \frac{4.574}{4 \text{ ang}}$$

$$V_{w_{2}} = 25.13 - 7.915$$

$$V_{w_{2}} = 17.215 \text{ m/s}$$

Work done by Impeller,

$$W = \frac{1}{9} V_{w_2} U_2$$

= $\frac{17.215 \times 25.13}{9.81}$
= $\frac{44.1 \text{ Nm/s}}{17.215}$

Reput :

4. A centrifugal pump delivers water against a net head of 14.5 meters and a design speed of 1000 rpm. The Vares are avoived back to an angle of 30° with the periphery. The Impetter diameter is 300 mm and outlet width 50 mm. Determine the discharge of the pump if Manometric Afficiency is 95%.

Given: Net head (Hm) = 14:5m Speed N = 1000 Y.p.m Vane angle at outlet p = 30° Diameter D2 = 300 mm = 0.30 m Outlet width B2 = 50 mm = 0.05 m Hanometric Efficiency. 7man = 95% = 0.95

Find :

Formula: $Q = TT D_{9} B_{2} \times V_{42}$ Solution: Tangential velocity of impeller at outlet(U_{2}) = $\frac{TTD_{1}}{60}$ $= \frac{TT \times 0.30 \times 1000}{60} \Rightarrow 15.70 \text{ m/s}$ $D_{man} = \frac{9 \text{ Hm}}{V_{w_{3} \times U_{2}}}$ $U_{R} = 15.70 \text{ m/s}$ $U_{R} = 15.70 \text{ m/s}$ $U_{R} = 15.70 \text{ m/s}$ $U_{R} = 15.70 \text{ m/s}$

From outlet velocity Exiangle, we have $\tan \varphi = \frac{V_{f_2}}{U_2 - V_{w_2}} \Rightarrow \tan 30^\circ = \frac{V_{f_2}}{(15.70 - 9.54)}$ $\tan 30^{\circ} = \frac{V_{f2}}{6.16}$; $V_{f2} = 6.16 \times 10^{\circ} 30^{\circ}$ V12 = 3.556 m/1 Discharge of the pump (Q) = II D, B2 × V12 = TIX 0.30x 0.55 x 3.55 = 0.1840 mº1s Renull: Discharge of the certrifugal pump is (Q) = 0.1840 m3/s 5. The length is diameter of a Suction pipe of a single acting reciprocating pump are In & 10cm respectively. The pump has a plunger of diameter 15 cm 28 a stroke length of 35cm. The Center of the pump is 3 m above the water Surface in the pump. The atmospheric premise head is 10.3m of water and pump is running at 36 r. p.m (16) [NOV / DEC - 2017] Determine, (i) Pressure head due to aculeration at the beginning of the suction stacke. (i) Man Pressure head due to acceleration, and. (ci) Pressure head in the cylinder at the beginning 18 at the end of the stroke. Given: Length of suction pipe (ls) = 5m. Dia. of suction pipe (ds) = 10 cm = 0.1m. : Area (as) = TT (d1) $= \prod_{i=1}^{n} (0.1)^2 = 0.007854 \text{ m}^2$

Dia of plunger D = 15cm = 0,15m.

$$\therefore Aua of Plunger A = \frac{\pi}{4} D^{2}$$

$$= \frac{\pi}{4} \times 0.15^{2}$$

$$= 0.01767m^{2}$$
Stroke length, $L = 35cm = 0.35m$

$$\therefore Crank Radius r = H_{2}$$

$$= \frac{0.35}{2} = 0.175m$$
Suction head $(h_{1}) = 3m^{2}$
Atmospheric pressure head, $H_{alm} = 10.3 \text{ mg}$ wate.
Speed $(N) = 35r.pm$.
Angular dipled of the crank \dot{u} .
 $w = \frac{2\pi N}{60} = \frac{2\pi \times 35}{60}$
 $us = 3.665 \text{ rad/s}.$
(i) The pressure head due to acceleration \dot{u} the Suetimpipe has $= \frac{l_{1}}{9} \times \frac{A}{4s} \times us^{2}r \cos 0$.
At the beginning of stroke. $0:0$ and hence $\cot 0 = 1$
 $h_{as} = \frac{l_{1}}{9} \times \frac{A}{4s} \times us^{2}r$
 $= \frac{5}{9.61} \times \frac{0.01767}{0.007454} \times 3.665^{2} \times D.175$
(ii) Man. pressure head due to acceleration in soution pipe $(h_{as})_{man} = \frac{l_{1}}{9} \times \frac{A}{4s} = \frac{w^{2}r}{0.007454}$

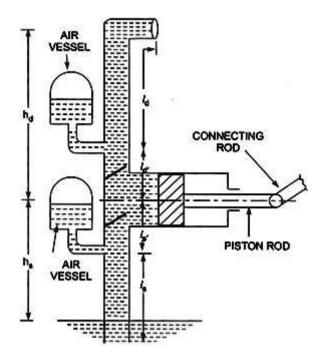
(iii) Premue head in the cylinder at the beginning of the Sution Stroke = he + has = 3 + 2,695 = 5,695. This premure head in the cylinder is below the atmospheric pressure head. ". Absolute pursure head in the? Hatm - has cylinder at the beginning of] = Hatm - has = 10.3 - 5.695 = 4.605 m of water Cabe) (iv) Simillarly, The premure head in the cylinder at the end of sultion stroke. = hs - has = 3 - 2,695 = 0.305 m Which is below the atmospheric pressure head. ". Abrolute premue head in the premue head cylinder at the end of suction stacked? Hain - has = 10.3 - 0.805 = 9.995 m of water (961.)

6(a) What is an air vessel? Describe the function of the air vessel for reciprocating pump with neat sketch. (8)

It is a closed chamber containing compressed air in the top portion and liquid (or water) at the bottom of the chamber. This is used to obtain a continuous supply of liquid at a uniform rate, to save a considerable amount of work in overcoming the frictional resistance in the suction and delivery pipes and to run the pump at high speed without separation.

The figure shows the single acting reciprocating pump to which air vessels are fitted to the suction and delivery pipes. The air vessels act like an

intermediate reservoir. During the first half of the stroke, the piston moves with acceleration, which means the velocity of water in the suction pipe is more than



the mean velocity and hence the discharge of water entering the cylinder will be more than the mean discharge. This excess quantity of water will be supplied from the air vessel to the cylinder in such a way that the velocity in the suction pipe below the air vessel is equal to mean velocity of flow. During the second half of the suction stroke, the piston moves with retardation and hence the velocity of flow n the suction pipe is less than the mean velocity of flow. Thus, the discharge entering the cylinder will be less than the mean discharge. The velocity of water in the suction pipe due to air vessel is equal to mean velocity of flow and discharge required in cylinder is less than the mean discharge. Thus the excess water flowing in suction pipe will be stored into air vessel, which will be supplied during the first half of the stroke.

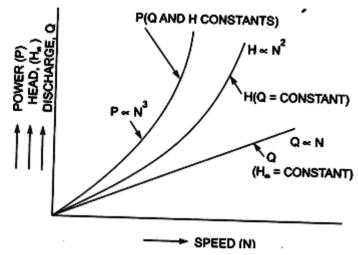
During the second half of the delivery stroke, the piston moves with retardation and the velocity of water in the delivery pipe will be less than the mean velocity. The water already stored into the air vessel will start flowing into the delivery pipe and the velocity of flow in the delivery pipe beyond the point to which air vessel is fitted will become equal to the mean velocity. Hence the rate of flow of water in the delivery pipe will be uniform.

6(b) Draw and discuss the characteristic curves of centrifugal pumps. (8)

Main characteristic curves

The main characteristic curves of a centrifugal pump consists of variation of head H_m , power and discharge with respect to speed. For plotting curves of manometric head versus speed, discharge, is kept constant. For plotting curves of discharge versus speed, manometric head H_m is constant

For plotting the graph of H_m versus speed N, the discharge is kept constant. From equation H α N².this means that head developed by pump is proportional to the N² hence the curve is a parabolic curve. P α N³. This means the curve is a cubic curve Q α N hence it is a straight line.



Operating characteristic curves

If the speed is kept constant. The variation of manometric head, power and efficiency with respects to the discharge gives the operating characteristics of the pump.

The input curve for pumps shall not pass through the origin. It will be slightly away from the origin on the y-axis, as even at zero discharge some power is needed to overcome mechanical losses.

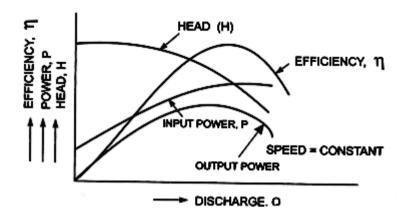
The head curve will have maximum value of head when discharge is zero.

The output power curve will start from origin as at Q=0, output power will be zero.

The efficiency curve will start from the origin as at $Q=0,\eta=0$

Constant Efficiency Curves

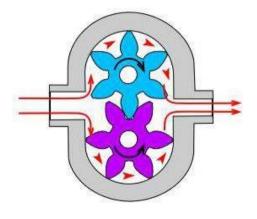
For obtaining constant efficiency curves for the pump, the head versus discharge curves and efficiency versus discharge curves for different speed are used. Fig shows the head versus discharge curves for different speeds. The efficiency versus discharge curves for the different speeds are as shown in Fig. by



combining these curves (H-Q curves and η –Q curves), constant efficiency curves are obtained

For plotting the constant efficiency curves (also known as iso -efficiency curves), horizontal lines representing constant efficiencies are drawn on the η -Q curves. The points, at which these lines cut the efficiency curves at various speed, are transferred to the corresponding H-Q curves. The points having the same efficiency are then joined by smooth curves. These smooth curves represent the iso efficiency curves.

7. Discuss the working of gear pump with its schematic (April/May 2017)



Gear pump-Schematic

Gear pump is a robust and simple positive displacement pump. It has two meshed gears revolving about their respective axes. These gears are the only moving parts in the pump. They are compact, relatively inexpensive and have few moving parts. The rigid design of the gears and houses allow for very high pressures and the ability to pump highly viscous fluids. They are suitable for a wide range of fluids and offer selfpriming performance. Sometimes gear pumps are designed to function as either a motor or a pump. These pump includes helical and herringbone gear sets (instead of spur gears), lobe shaped rotors similar to Roots blowers (commonly used as superchargers), and mechanical designs that allow the stacking of pumps.

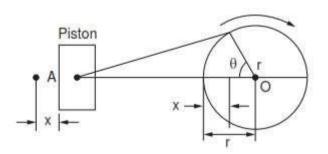
Construction:

One of the gears is coupled with a prime mover and is called as driving gear and another is called as driven gear. The rotating gear carries the fluid from the tank to the outlet pipe. The suction side is towards the portion whereas the gear teeth come out of the mesh. When the gears rotate, volume of the chamber expands leading to pressure drop below atmospheric value. Therefore the vacuum is created and the fluid is pushed into the void due to atmospheric pressure. The fluid is trapped between housing and rotating teeth of the gears. The discharge side of pump is towards the portion where the gear teeth run into the mesh and the volume decreases between meshing teeth. The pump has a positive internal seal against leakage; therefore, the fluid is forced into the outlet port. The gear pumps are often equipped with the side wear plate to avoid the leakage. The clearance between gear teeth and housing and between side plate and gear face is very important and plays an important role in preventing leakage. In general, the gap distance is less than 10 micrometers.

8. Derive the expression for pressure head due to acceleration in the suction and delivery pipes of the reciprocating pumps. (Nov/Dec 2016)

The piston in the reciprocating pump has to move from rest when it starts the suction stroke. Hence it has to accelerate. The water in the suction pipe which is also not flowing at this point has to be accelerated. Such acceleration results in a force which when divided by area results as pressure. When the piston passes the mid-point, the velocity gets reduced and so there is retardation of the piston together with the water in the cylinder and the pipe. This again results in a pressure. These pressures are

called acceleration pressure and is denoted as head of fluid (h = $P/\rho g$) for convenience.



Configuration of piston crank

Let ω be the angular velocity.

Then at time t, the angle travelled $\theta = \omega t$

Distance $x = r - r \cos \theta = r - r \cos \omega t$

Velocity at this point,

$$V = \frac{dx}{dt} = \omega r \sin \omega t \qquad (1)$$

The acceleration at this condition

$$x = \frac{dx}{dt} = \omega^2 r \cos \omega t \tag{2}$$

This is the acceleration in the cylinder of area A. The acceleration in the pipe of area a

is,
$$= \frac{4}{a} \omega^2 r \cos \omega t \qquad (3)$$

Accelerating force = mass \times acceleration

Mass in the pipe =
$$\rho$$
 al = $\frac{\gamma a l}{g}$
Acceleration force = $\frac{\gamma a l}{g} x \frac{A}{a} \omega^2 r \cos \omega t$ (4)
Pressure = force/area
= $\frac{\gamma a l}{g} x \frac{1}{a} x \frac{A}{a} \omega^2 r \cos \omega t$
= $\frac{\gamma l}{g} x \frac{A}{a} \omega^2 r \cos \theta$
Head = Pressure/ γ
 $\mathbf{h}_{\mathbf{d}} = \frac{l}{g} x \frac{A}{a} m^2 r \cos \theta$ (5)

This head is imposed on the piston in addition to the static head at that condition.

PART – C

1. In a single acting reciprocating pump with plunger diameter of 120 mm and stroke of 180 mm running at 60 rpm, an air vessel is fixed at the same level as the pump at a distance of 3 m. The diameter of the delivery pipe is 90 mm and the length is 25 m. Friction factor is 0.02. Determine the reduction in accelerating head and the friction head due to the fitting of air vessel.

Without air vessel:

$$\mathbf{h}_{\mathbf{d}} = \frac{l}{g} \times \frac{A}{a} m^2 r = \frac{25}{9.81} \times \frac{0.12^2}{0.09^2} \left(\frac{2\pi \times 60}{60}\right)^2 \times 0.09$$
$$= 16.097 \text{ m}$$

With air vessel:

$$h'_{ad} = \frac{3}{9.81} x \frac{0.12^2}{0.09^2} \left(\frac{2\pi x \, 60}{60}\right)^2 x 0.09 = 1.932 \text{ m}$$

Reduction = 16.097 - 1.932 = 14.165 m

Fitting air vessel reduces the acceleration head.

Without air vessel:

Friction head,
$$h_f = \frac{4flv^2}{2ad} = \frac{4fl}{2gd} \left(\frac{A}{a} \omega r \sin\theta\right)^2$$

At $\theta = 90^\circ$,

$$h_{\text{fmax}} = \frac{4 \ x \ 0.02 \ x \ 25}{2 \ x \ 9.81 \ x \ 0.09} \left(\frac{0.12}{0.09} \ \frac{2\pi \ x \ 60}{60} \ x \ 0.09 \ x \ 1\right)^2 = 1.145\text{m}$$

With air vessel, the velocity is constant in the pipe.

Velocity, V =
$$\frac{LAN}{60} \times \frac{4}{\pi d^2} = \frac{\pi \times 0.12^2}{4} \times \frac{0.18 \times 60 \times 4}{60 \times \pi \times 0.09^2} = 0.102 \text{ m/s}$$

Friction head, h_f = $\frac{4 \times 0.02 \times 25 \times 0.102^2}{2 \times 9.81 \times 0.09} = 0.012 \text{ m}$

Percentage saving over maximum, $=\frac{1.145-0.012}{1.145} \times 100 = 99\%$

Thus, Air vessel reduces the frictional loss.

UNIT -IV

TURBINES

1. Define volumetric efficiency?

(Nov/Dec14), (Nov/Dec15)

It is defined as the volume of water actually striking the buckets to the total water Supplied by the jet

2. Write short notes on Draft tube? (Nov/Dec15)

It is a gradually increasing area which connects the outlet of the runner to the tail race. It is used for discharging water from the exit of the turbine to the tail race.

3. How are hydraulic turbine classified? (May/june14,April/May 11)

- **1.** According to the type of energy
- **2.** According to the direction of flow
- **3.** According to the head at inlet
- **4.** According to the specific speed of the turbine

4. What is mean by hydraulic efficiency of the turbine? (Nov/Dec13,12)

It is ratio between powers developed by the runner to the power supplied to the water jet

5. Define specific speed of the turbine (April/may 08, May/June 07)

The speed at which a turbine runs when it is working under a unit head and develop unit power

6. What is meant by governing of a turbine?

It is defined as the operation by which the speed of the turbine is kept constant under all conditions of working. It is done by oil pressure governor.

7. List the important characteristic curves of a turbine

- a. Main characteristics curves or Constant head curves
- b. Operating characteristic curves or Constant speed curves
- c. Muschel curves or Constant efficiency curves

8. Define gross head and net or effective head.

Gross Head: The gross head is the difference between the water

level at the reservoir and the level at the tailstock.

Effective Head: The head available at the inlet of the turbine.

9. What is the difference between impulse turbine and Reaction turbine?

(April/May 2011,08)

S.No	Reaction turbine	Impulse turbine
1.	Blades are in action at all the time	Blades are only in action when they are in front of nozzle
2.	Water is admitted over the circumference the wheel	Water may be allowed to enter a part or whole of the wheel circumference

10. Give example for a low head, medium head and high head turbine

(Nov/Dec 09)

Low head turbine – Kaplan turbine

Medium head turbine – Modern Francis

High head turbine – Pelton wheel

11. Explain the type of flow in Francis turbine? (Nov/Dec 2016)

The type of flow in Francis turbine is inward flow with radial discharge at outlet.

12. How do you classify turbine based on flow direction and working medium? (April/May 2017)

According to the direction of flow turbines are classified into

- (i) Tangential flow turbine
- (ii) Radial flow turbine
- (iii) Axial flow turbine
- (iv) Mixed flow turbine

According to the working medium turbines are classified into

- (i) Gas turbine
- (ii) Water turbine
- (iii) Steam turbine

PART-B

1. A Petton wheel has a mean bucket speed of 10 metres per Second. with a jet of water flowing at rate of 700 l/s. Under a head of 30 meters. The bucket deflect the jet through an angle 160°. Calculate power again by surver and hydraulic efficiency of turbine. dsmore co. efficient of Velocity as 0.98. [16] [NOV/DEC - 2012]

Given:

$$U = U_1 = U_2 = 10 \, m/s.$$

$$Q = 700 \, L/s = 0.7 \, m^3/s.$$

$$H = 30 \, m.$$

$$Q = 180^{\circ} - 160^{\circ} = 20^{\circ}$$

$$C_V = 0.98.$$

formula: (i) Power = Workdone by the jet / second KW 1000 (ii) Hydraulic Afficiency (7,) = 2[Vw,+Vw_2]×U (V3)

Solution: (i) The Velocity of Set
$$V_1 = C_V \sqrt{2gH}$$
.
 $V_1 = C_V \sqrt{2gH}$.
 $= 0.98 \sqrt{2x9(81x30)} = 23,777 m/s$
 $V_1 = 23.777 m/s$
 $V_1 = 23.777 m/s$
 $V_{r_1} = V_1 - U_1$
 $V_{r_1} = 1, 23.777 m/s$
 $V_{w_1} = 13.777 m/s$

From out let velocity triangle,

$$V_{w_2} = V_{r_1} = 13, \# \# m/s$$

$$V_{w_2} = V_{r_2} \cos \varphi - u_2$$

$$= 13.77 \cos 20^\circ - 10.0$$

$$V_{w_2} = 2.94 m/s$$

(ii) Work done by the jet per second on the runner is given by equation.
 = PaV, [Vw, + Vw2] × U
 = 1000 × 0.7 × [23.77 + 2.94] × 10
 = 186970 Nm/s [:' aV, = Q = 0.7 m³/s]

(cli) powers given to turbine = work done /sec KW

(iv) The hydraulic Afficiency of the
$$y = \frac{2[V_{w_1} + V_{w_2}]_{v_1}}{(V_1)^2}$$

 $(V_1)^2$
 $(V_1)^2$
 $\frac{2[28.77 + 2.94]_{x_10}}{(28.77)^2}$
 $\Rightarrow 0.9454 (08) 94,54 7$.

2. In an Inward radial flow turbine, water enters at an angle of 22° to wheel tangent to outer sin and leaves at 3 m/s. Inner diameter 300 mm & outer dia boo mm. Speed is 300 pm. The discharge through the surrer radial.

Guide blade angles $\mathscr{S} = \mathscr{d}\mathscr{L}^{\mathcal{P}}$. Velocity of flow $V_{f_1} = V_{f_2} = \mathscr{S}m/s$. $D_1 = \mathscr{B}oomm ; 0.3m$. $D_2 = \mathscr{B}oomm ; 0.6m$. $N = \mathscr{B}oo\mathfrak{P}pm$. $\beta = 90^\circ \mathscr{S} V_{w_2} = 0$ Julet width $(\beta_1) = 1\mathfrak{S}omm = 0.15mm$.

Solu: Tangential velocity of wheel at Inlet. $u_{1} = \frac{TD_{1}N}{60} = \frac{T1 \times 0.3 \times 300}{60}$ $u_{1} = A.71 \text{ m/s.}$ Tangential Velocity of wheel at outlet. $u_{2} = \frac{TD_{2}N}{60} = \frac{T1 \times 0.6 \times 300}{60}$ $u_{2} = 9.43 \text{ m/s.}$ Absolute velocity of water at Inlet. $V_{1} = \frac{V_{3}}{Sinco} = \frac{3}{Sin22} = 8.0084 \text{ m/s.}$ Velocity of wheel at Inlet. $V_{w_{1}} = V_{1} (\cos d) = 8.0084 \times \cos 22$ $V_{w_{1}} = 7.4853 \text{ m/s.}$

The Discharge
$$Q = TT D_1 B_1 V_{f_1}$$

= $TT \times 0.3 \times 0.15 \times 3$
= $0.4 R41 m^3/s$.
For summer blade angles;
From Inlet Velocity Inlangles, $V_2 = V_{f_1} = V_{f_2}$
tano = $\frac{V_{f_1}}{V_{w_1} - u_1} = \frac{3}{T.4253 - 4.71}$
tano = 1.1048
 $Q = 47.85^\circ$
 $V_1 = V_{f_1}$

Power developed,

$$P = \frac{PQ(V_{w_1} \times u_1)}{(000)}$$

$$= (000 \times 0.4241 (7.4253 \times 4.71))$$

$$= 14.83 \text{ Kw}$$

Result :

(i) Inlet velocity triangle
$$y = 47.85^{\circ}$$

outlet velocity triangle
 $\varphi = 17.65^{\circ}$

(ii) power developed (p) = 14,83 KW.

A Kaplan turbine working Under a head of 20m 3. developes 15 NW brake. The hub diameter 1.5m. summer dianeter is 4m. The guide black angle 7h = 0.9 \$ 70 = 0.8 Find sunner vare angles & [Apr/may - 2010] turbine speed. [16]

folution :

$$H = lom.$$

$$P = 15MW = 15000 KW.$$

$$Do = 4m.$$

$$Db = 1.5m$$

$$\alpha = 80^{\circ}$$

$$\gamma_{h} = 0.9 = 90\%.$$

$$\eta_{0} = 0.8 = 80\%.$$

$$\beta = 90^{\circ} s Vw_{2} = 0$$
Find:
$$Q = ?$$
Vane angles:
$$P = ?$$
turbine speed N = ?

Formula:

? = 0.80
(i) Vane angles
$$\tan \alpha = \frac{V_{F,i}}{V_{i0,i}}$$

 $\tan \varphi = \frac{V_{F,2}}{U_2}$; $\tan \varphi = \frac{V_{F,i}}{V_{i0,i}-U_1}$
(ii) mi speed of the trebine $N = ?$

Solution:

we know than

$$\begin{aligned}
\mathbf{q} &= \frac{11}{4} \left(D_{a}^{2} - D_{b}^{2} \right) \times V_{f,i} \\
\mathbf{q}_{S,5b} &= \frac{11}{4} \left(A^{2} - 1.5^{2} \right) \times V_{f,i} \\
\mathbf{V}_{f,i} &= 8.8487 \text{ m/s} \\
\hline
\mathbf{V}_{i,i} &= \frac{1}{4} \left(\frac{1}{2} - \frac{1}{2} + \frac{1$$

$$\frac{V_{W_1} - u_1}{V_{W_1} - u_1} = \frac{8.8487}{(5.33 - 11.5)} = 2.8216$$

$$tan 0 = 2.3216$$

 $0 = tan^{-1} (2.3216)$
 $= 66.69$
 $0 = 66.69^{\circ}$

For Kaplan turbine,

$$u_1 = u_2 = 11.518 \, m/s$$

 $V_{F_1} = V_{F_2} = 8.8487 \, m/s$
 $\tan \varphi = \frac{V_{G_2}}{u_2} = 0.7682$.
 $\varphi = \tan^{-1}(0.7682) = 37.53$

.

$$u_1 = \frac{\pi D N}{60}$$

$$(1.5) = \frac{\pi \times 4 \times N}{60}$$

$$N = 54.997 \text{ rpm}.$$

Republic :

4. A Francis turbine developing 16120 KW Ordera head of
260 m Runs at 600 spm. The Runner outside diameter is
1500 mm as the width is 135 mm. The flow Rate is
$$7m^3/s$$
.
The exit Velocity at the deaft tube outlet is 16 m/s.
The exit Velocity at the deaft tube outlet is 16 m/s.
The exit velocity at the deaft tube outlet is 16 m/s.
Assuming zero which velocity at enit. and neglecting
blade thickness. determine the overall st hydraulic
blade thick

$$V_{2} = V_{f_{2}} = 16 m/s$$
; $V_{w_{2}} = 0$.

To Find !

Solution :

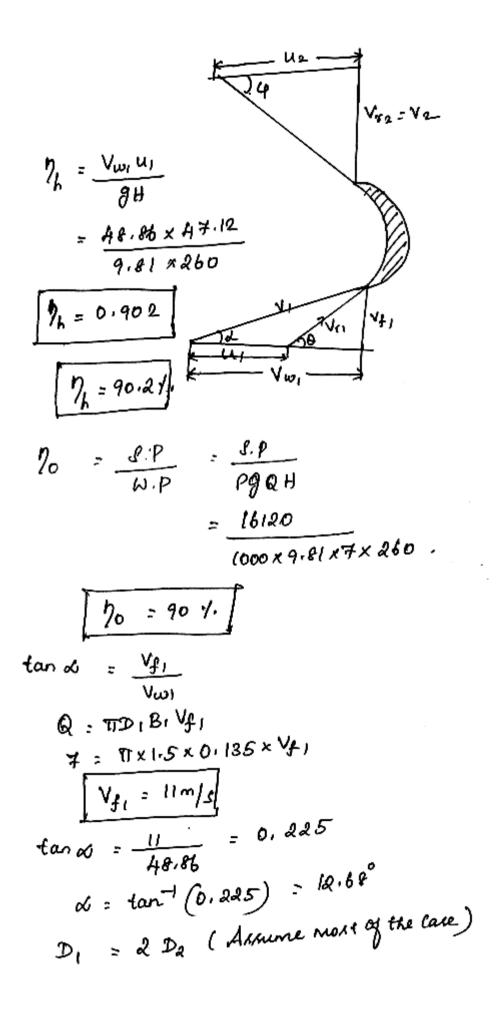
$$u_{1} = \frac{TD_{1}N}{60} = \frac{TX_{1.5} \times 600}{60}$$

$$= 47.12 \text{ m/s} \text{ .}$$
Power developed (p) = $\frac{PQ}{C00} \frac{Vw_{1}u_{1}}{C000}$

$$V = 16120 = \frac{1000 \times 7 \times Vw_{1} \times 47.12}{C000}$$

$$Vw_{1} = 48.86 \text{ m/s}$$

ł



 $D_{2} = \frac{1.5}{2} = 0.75$ $U_{2} = \frac{1100}{60} = \frac{1100}{60} = 23.56 \text{ m/s}$ $U_{2} = \frac{1000}{60} = 0.679$ $fan \varphi = \frac{18}{23.56} = 0.679$ $\varphi = 4an^{-1} (0.679) = 34^{\circ} \frac{18}{(\varphi = 34^{\circ} 18)}$ Penult: $Po = 90.27.5 \text{ m/s} = 12.68^{\circ}$ $\varphi = 34^{\circ} 18^{\circ}$

5. With a neat sketch, explain the construction and working of Pelton wheel. [APR./MAY 2008]

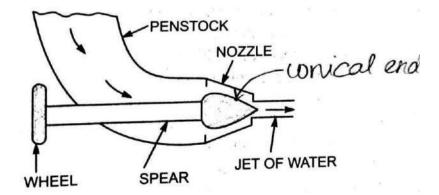
Pelton turbine is a tangential flow impulse turbine. It is named after L.A.Pelton, an American engineer. This turbine is used for high heads.

MAIN PARTS:

- 1. Nozzle and flow regulating valve
- 2. Runner and buckets
- 3. Casing
- 4. Breaking jet

1. Nozzle and flow regulating valve

The nozzle increases the kinetic energy of water flowing through the penstock. At the outlet of the nozzle, the water comes out in the form of jet and strikes the bucket of the runner. The amount of water striking the buckets of the runner is controlled by providing a spear in the nozzle. The spear is a conical needle which can be operated manually. When the spear is pushed forward or backward into



the nozzle the amount of water striking the runner is reduced or increased.

2. Runner and buckets

The runner consists of a circular disc with a number of bucket evenly spaced round its periphery. The shape of the bucket is of semi ellipsoidal cups. Each bucket is divided into two symmetrical parts by a dividing which is known as splitter. The splitter divides the jet into two equal parts and the jet comes out at the outer edge of the bucket.

The bucket is made up of cast iron, cast steel bronze or stainless steel depending upon the head at the inlet of the turbine.

3. Casing:

The function of casing is to prevent the splashing of the water and to discharge water to tail race. It also acts as a safeguard against accident.

It is made up of cast iron or fabricated steel plates.

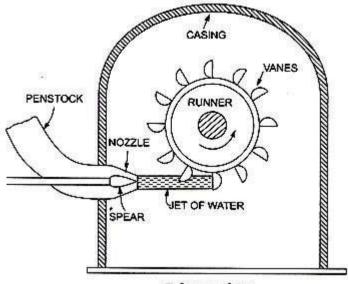
4. Breaking jet:

When the nozzle is completely closed by moving the spear in the forward direction, the amount of water striking the runner reduces to zero. But the runner due to inertia goes on revolving for a long time. To stop the runner in a short time, a small nozzle is provided which directs the jet of water on the back of the vanes. This jet of water is called breaking jet.

Working:

The water from the reservoir flows through the penstocks at the outlet of which a nozzle is fitted. The nozzle increases the kinetic energy of water flowing through the penstock. At the outlet of the nozzle, the water comes out in the form of jet and strikes the bucket of the runner.

The water flows along the tangent to the path of rotation of the runner. The runner revolves freely in air. The water is in contact with only a part of the runner at a time, and throughout its action on the runner and in its subsequent flow to the tail race, the water is at atmospheric pressure. Casing is to prevent the splashing of the water and to discharge water to tail race.



Pelton turbine.

6. Draw the characteristic curves of the turbines. Explain the significance?

Characteristics curves of a hydraulic turbine are the curves, with the help of which the exact behavior and performance of the turbine under different working conditions can be obtained. These curves are plotted from the results of the tests performed on the turbine.

The important parameters which are varied during a test on a turbine:

1.Speed (N) 2.Head(H) 3. Discharge(Q) 4.Power(P)

5.overall deficiency(η_0) 6. Gate opening

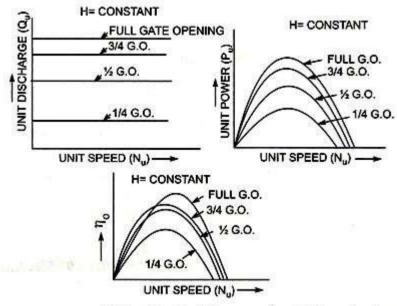
Speed (N), Head(H), Discharge(Q) are independent parameters. One of the parameters are kept constant and the variation of the other four parameters with respect to any one of the remaining two independent variables are plotted and various curves are obtained. These curves are called characteristics curves. The following are the important characteristic curves of a turbine.

1. Main characteristics curves or constant head curves.

- 2. Operating characteristics curves or constant speed curves
- 3. Muschel curves of constant efficiency curves

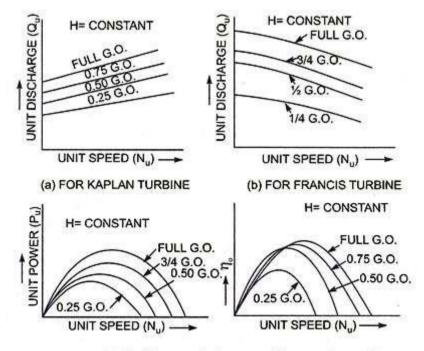
MAIN CHARACTERISTICS CURVES OR CONSTANT HEAD CURVES.

Main characteristics curves are obtained by maintaining a constant head and a constant gate opening on the turbine. The speed of the turbine is varied by changing load on the turbine. For each value of the speed , the corresponding values of the power (P) and discharge(Q) are obtained. Then the overall efficiency (η_o) for each value of the speed is calculated. From these readings the values of unit speed (N_u) , unit power (P_u) , and unit discharge (Q_u) are determined. Main characteristics curves of a Pelton wheel as shown below.



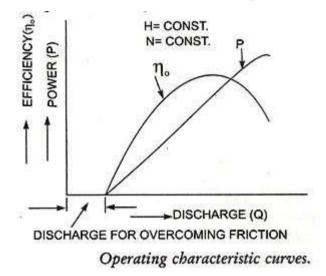
Main characteristic curves for a Pelton wheel.

Main characteristics of a Kaplan and reaction turbine as shown below.



Main characteristic curves for reaction turbine. OPERATING CHARACTERISTICS CURVES OR CONSTANT SPEED CURVES :

Operating Characteristics Curves are plotted when the speed on the turbine is constant. There are three independent parameters namely N, H and Q. For operating characteristics N and H are constant and hence the variation of power and efficiency with respect to discharge Q are plotted. The power curve for turbines shall not pass through the origin because certain amount of discharge is needed to produce power to overcome initial friction. Hence the power and efficiency curves will be slightly away from the origin on the x-axis as to overcome initial friction certain amount of discharge will be required.

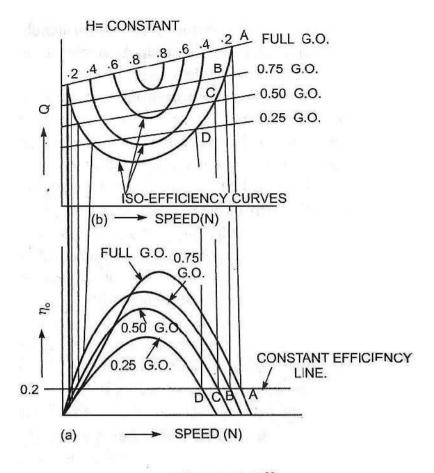


MUSCHEL CURVES OF CONSTANT EFFICIENCY CURVES :

These curves are obtained from the speed Vs efficiency and speed Vs discharge curves for different gate openings. For a given efficiency, from the N_u vs η_0 curves, there are two speeds. From the N_u vs Q_u curves, corresponding to two values of speeds there are two values of discharge. If the efficiency is maximum there is only one value. These two values of speed and two values of discharge corresponding to a particular gate opening are plotted.

The procedure is repeated for different gate opening and the curve Q vs N are plotted. The points having the same efficiency are iso-efficiency curves. These curves are useful to determine the zone of constant efficiency and for predicting the performance of the turbine at various efficiencies.

Horizontal lines representing the same efficiency are drawn on the η_0 speed curves. The points at which these lines cut the efficiency curves at various gate opening are transferred to the corresponding Q- speed curves. The points having the same efficiency are then joined by smooth curves. These smooth curves represent the iso-efficiency curve.



Constant efficiency curve.

7. Explain the working of Kaplan turbine. Construct its velocity triangles.

(Nov/Dec 2016)

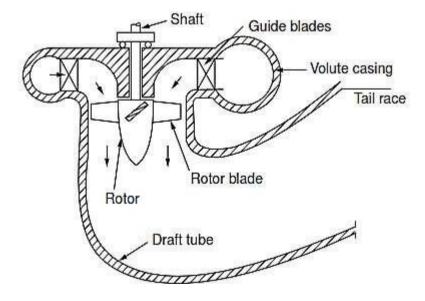
The popular axial flow turbines are the Kaplan turbine and propeller turbine. In propeller turbine the blades are fixed. In the Kaplan turbines the blades are mounted in the boss in bearings and the blades are rotated according to the flow conditions by a servomechanism maintaining constant speed. In this way a constant efficiency is achieved in these turbines. The system is costly and where constant load conditions prevail, the simpler propeller turbines are installed. There are many locations where large flows are available at low head. In such a case the specific speed increases to a higher value. In such situations axial flow turbines are gainfully employed. A sectional view of a kaplan turbines in shown in figure. These turbines are suited for head in the range 5 - 80 m and specific speeds in the range 350 to 900. The water from supply pipes enters the spiral casing as in the case of Francis turbine. Guide blades direct the water into

the chamber above the blades at the proper direction. The speed governor in this case acts on the guide blades and rotates them as per load requirements.

The flow rate is changed without any change in head. The water directed by the guide blades enters the runner which has much fewer blades (3 to 10) than the Francis turbine. The blades are also rotated by the governor to change the inlet blade angle as per the flow direction from the guide blades, so that entry is without shock. As the head is low, many times the draft tube may have to be elbow type. The important dimensions are the diameter and the boss diameter which will vary with the chosen speed. At lower specific speeds the boss diameter may be higher.

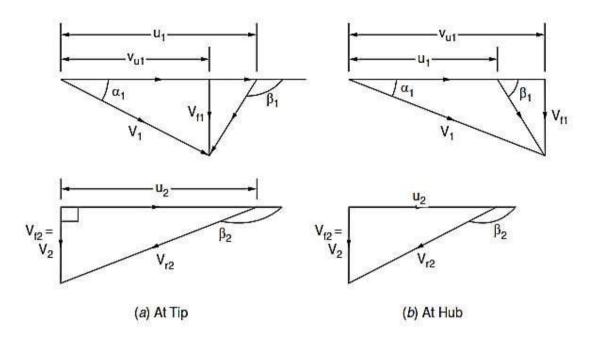
The number of blades depends on the head available and varies from 3 to 10 for heads from 5 to 70 m. As the peripheral speed varies along the radius (proportional to the radius) the blade inlet angle should also vary with the radius. Hence twisted type or Airfoil blade section has to be used. The speed ratio is calculated on the basis of the tip speed as $\emptyset = \frac{u}{\sqrt{2gH}}$ and varies from 1.5 to

2.4. The flow ratio lies in the range 0.35 to 0.75.



Sectional view of Kaplan turbine

Velocity triangles



PART-C

1. The head available at a location was 1500 m. It is proposed to use a generator to run at 750 rpm. The power available is estimated at 20,000 kW. Investigate whether a single jet unit will be suitable. Estimate the number of jets and their diameter. Determine the mean diameter of the runner and the number of buckets.

Solution: The specific speed is calculated to determine life number of jets, $N_{S} = \frac{750}{60} \sqrt{\frac{20,000 \times 10^{3}}{1500^{5/4}}}$ $N_{S} = 5.99$ So a Single jet will be suitable. The orerall efficiency is assumed as 0.87. $20,000 \times 10^{3} = 0.87 \times Q \times 1000 \times 9.81 \times 1500$ $\Rightarrow Q = 1.56225 m^{3}/s$

To determine the jet velocity, the value of
$$C_v$$
 is
required. It is assumed as 0.97.
 $V = 0.97 \sqrt{2.9H}$
 $= 0.97 \sqrt{2.9H}$
 $V = 166.4 \text{ m}/\text{p}$
We know, $Q = A.V$
 $1.56225 = \frac{\Lambda}{H} d^2 \times 166.4$
 $\Rightarrow d = 0.1093 \text{ m}$

Assume,
$$\phi = 0.46$$

 $4 = 166.4 \times 0.46$
Also, $4 = \frac{7.0N}{60}$
 $\Rightarrow D = \frac{604}{\pi N}$
 $= \frac{60 \times 166.4 \times 0.46}{\pi \times 750}$
 $\boxed{D = 1.95m}$
Number of buckets, $= z. \frac{D}{2d} + 15$
 $= \frac{1.95}{2\times 0.1093} + 15$
 $= 24$

2. At a location selected to install a hydroelectric plant, the head is estimated as 550 m. The flow rate was determined as 20 m 3m/s. The plant is located at a distance of 2 m from the entry to the penstock pipes along the pipes. Two pipes of 2 m diameter are proposed with a friction factor of 0.029. Additional losses

.

amount to about 1/4th of frictional loss. Assuming an overall efficiency of 87%, determine how much single jet unit running at 300 rpm will be required.

Solution:
Specific speed
Net bead = Head available - low in head
Friction LONE =
$$\frac{\int LV_p^2}{2gp}$$

 $Q = V_p \times A_p \times number of pipes$
 $Q = Rom^3 | s$ (given).
 $\Rightarrow V_p = \frac{20}{(\frac{\pi}{4} + 2^{k_1})} \times 2$
 $V_p = 3.183 \text{ m/s}$
 $L = 2000 \text{ m}$, $f = 0.029$
 $h_f = \frac{0.029 \times 2000 \times 3.183^{k_1}}{2x 9.81 \times 2}$
 $h_f = 14.9p \text{ ms}$.
Total Loss of head = $(1 - \frac{1}{4}) \times 14.98$
 $= \frac{5^{-1}}{4} \times 44.98$
 $= 18.72 \text{ ms}$
 $\therefore \text{ Net head} = 550 - 18.72$
 $= 591.28 \text{ ms}$
 $\therefore \text{ Power, } p = NQP9H$
 $p = 0.87 \times 20 \times 1000 \times 9.81 \times 521.28$
 $p = 9.06763 \times 10^{2} \text{ ms}$
Specific speed, $N_g = \frac{300}{60} \cdot \sqrt{90.696 \times 10^{2}}$
 $N_g = 18.667$

Suitability of single jet unit

$$V_{j} = C_{v} \sqrt{2^{2}gH}$$

$$= 0.98 \sqrt{2^{2}x9.81 \times 5^{2}1.28}$$
Velocity of 2 V_{j} = 100.05 m/s
jet J.
Discharge, Q = A.V_{j}
$$= \frac{T}{4} d^{2} \times V_{j}$$

$$d = \left(\frac{4Q}{T} V_{j}\right)^{1/2}$$

$$d = \left(\frac{4Q}{T} V_{j}\right)^{1/2}$$

$$d = 0.5 m$$
 (high)
Also, $\frac{TDN}{60} = 0.46 \times 100.05$

$$D = 2.93 m$$

Jet speed ratio =
$$\frac{2.95}{0.5}$$

= 6 (10w)

If then d = 0.29 m
then d = 0.29 m
jet speed ratio = 10 (Suitable)
Ns =
$$\frac{300}{60} \sqrt{\frac{90.6863 \times 10^{3}}{531.28^{51}9}}$$

No= 10.77 Hence a three jet unit can be suggested.

UNIVERSITY QUESTION PAPERS

1. <u>CE 6451-APRIL/MAY 2017</u>

Reg. No. :

Question Paper Code : 71563

B.E./B.Tech. DEGREE EXAMINATION, APRIL/MAY 2017.

Third/Fourth Semester

Mechanical Engineering

CE 6451 — FLUID MECHANICS AND MACHINERY

(Common to Aeronautical Engineering, Automobile Engineering, Industrial Engineering, Industrial Engineering and Management, Manufacturing Engineering, Mechanical and Automation Engineering, Mechatronics Engineering, Production Engineering)

(Regulations 2013)

Time : Three hours

Maximum : 100 marks

Answer ALL questions.

PART A —
$$(10 \times 2 = 20 \text{ marks})$$

- 1. Define Viscosity and what is the effect due to temperature on liquid and gases.
- 2. Calculate the height of capillary rise for water in a glass tube of diameter 1mm?
- 3. What are equivalent pipes? Mention the equation used for it.
- 4. Define Boundary Layer.
- 5. Explain the types of Similarities.
- 6. Write the expression for Mach number and state its application.
- 7. Explain the purpose of Air Vessel and in which pump it is used?
- 8. Define cavitation and its effects.

9. How do you classify turbines based on flow direction and working medium?

10. What is meant by Governing of Turbines?

- 11. (a)
- (i) Calculate the dynamic viscosity of an oil, which is used for lubrication between a square plate of size $0.8 \text{ m} \times 0.8 \text{ m}$ in an inclined plane with an angle of inclination 30° to the horizontal. The weight of the square plate is 300N and it slides down the inclined plane with a uniform velocity of 0.3 m/s. The thickness of oil film is 1.5mm. (8)
- (ii) An oil of specific gravity 0.8 is flowing through a venturimeter having inlet diameter 20 cm and throat diameter 10 cm. The oil-mercury differential manometer shows a reading of 25 cm. Calculate the discharge of oil through the horizontal venturimeter. Take $C_d = 0.98$. (5)

Or

- (b) Derive the expression of Bernoulli's equation from the Euler's equation and state the assumptions made for such a derivation? (13)
- 12. (a) (i) A fluid of viscosity 0.7 Pa.s and specific gravity 1.3 is flowing through a pipe diameter 120 mm. The maximum shear stress at the pipe value is 205.2 N/m². Determine the pressure gradient, Reynolds number and average velocity? (9)
 - (ii) A crude oil of kinematic viscosity 0.4 strokes is flowing through a pipe of diameter 300mm at the rate of 300 litres per sec. Find the head lost due to friction for a length of 50 m of the pipe. Take Coefficient of friction as 0.006.

Or

- (b) For a flow of viscous fluid flowing through a circular pipe under laminar flow conditions show that the velocity distribution is a parabola. And also show that the average velocity is half of the maximum velocity. (13)
- 13. (a) A 1:100 model is used for model testing of ship. The model is tested in wind tunnel. The length of ship is 400 m. The velocity of air in the wind tunnel around the model is 25 m/s and the resistance is 55N. Determine the length of model. Also find the velocity of ship as well as resistance developed. Take density of air and sea water as 1.24 kg/m³ and 1030 kg/m³. The kinematic viscosity of air and seawater are 0.018 stokes and 0.012 stokes respectively. (13)

Or

(b) Using Buckingham's π theorem, show that the velocity through a circular orifice is given by $V = \sqrt{2gH\phi} \left[\frac{D}{H}, \frac{\mu}{\rho vH}\right]$, where H is the head causing flow D is the diameter of the crifice. μ is coefficient of viece it.

causing flow, D is the diameter of the orifice, μ is coefficient of viscosity, ρ is the mass density and g is the acceleration due to gravity. (13)

2

- (a) (i) A Single acting reciprocating pump running at 50 RPM delivers 0.01 m³/s of water. The diameter of the piston is 200mm and stroke length 400 mm. Determine
 - (1) The theoretical discharge of the pump
 - (2) Coefficient of discharge
 - (3) Slip and Percentage slip of the pump. (8)
 - (ii) Discuss the working of Gear pump using its schematic. (5)

Or

- (b) A Centrifugal pump having outer diameter equal to two times the inner diameter and running at 1000 rpm works against a head of 40m. The velocity of flow through the impeller is constant and equal to 2.5 m/s. The vanes are set back at angle of 40° at outlet. If the outer diameter of the impeller is 500 mm & width at outlet is 50 mm determine (i) Vane angle at inlet, (ii) Manometric efficiency, (iii) Workdone by impeller on water per second. (13)
- 15. (a) (i) A kaplan turbine runner is to be designed to develop 9100 kW. The net available head is 5.6m. If the speed ratio = 2.09, flow ratio = 0.68, overall efficiency = 86% and the diameter of the boss is 1/3 the diameter of the runner. Find the diameter of the runner, its speed and the specific speed of the turbine? (8)

(ii) Explain the Performance Characteristics curves of turbine. (5)

Or

(b) The following data is given for a Francis turbine. Net head H = 60 m, Speed N = 700 RPM, Shaft power 294.3 kw, Overall efficiency 84%, Hydraulic efficiency 93%. Flow ratio = 0.2, breadth ratio n = 0.1, Outer diameter of the runner is two times inner diameter of the runner. The thickness of vanes occupies 5% of circumference area of the runner. Velocity of flow is constant at inlet and outlet and the discharge is radial at outlet. Determine (i) Guide blade angle, (ii) Runner vane angle at inlet and outlet, (iii) Diameter of runner inlet and outlet, (iv) Width of wheel at inlet.

PART C — $(1 \times 15 = 15 \text{ marks})$

16. (a) A liquid has a specific gravity of 0.72. Find its density, specific weight and its weight per litre of the liquid. If the above liquid is used as the lubrication between the shaft and the sleeve of length 100mm. Determine the power lost in the bearing, where the diameter of the shaft is 0.5 m and the thickness of the liquid film between the shaft and the sleeve is 1 mm. Take the viscosity of fluid as 0.5 N-s/m² and the speed of the shaft rotates at 200 rpm. (15)

3

(b) For a high head storage capacity dam of net head 800 m, it has been decided to design and install a Pelton wheel for generating power of 13,250 kw running at a speed of 600 RPM, if the coefficient of jet is 0.97 Speed Ratio = 0.46 and the Ratio of jet diameter is 1/15 of the wheel diameter calculate (i) Number of jets, (ii) Diameter of jets, (iii) Diameter of Pelton wheel, (iv) No of buckets and (v) Discharge of one jet. (15)

.